

# Flying of vector particles from a parity breaking (Chern-Simons) medium to vacuum and back

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A.A., S.Kolevator, R.Soldati, JHEP 11 (2011) 007

- ▶ **Maxwell-Chern-Simons Electrodynamics: possible manifestation**
  - a. **Large-scale universe or galaxies:** Carroll-Field-Jackiw model (1990) and cosmic birefringence. Spontaneous generation of MCS Electrodynamics by axion condensation, A.A., R.Soldati (1995).
  - b. **Parity breaking (PB) in a finite volume:** fireballs in heavy ion collisions with a non-zero topological charge and/or neutral pion condensate, chiral magnetic effect, D.Kharzeev, L. McLerran, A Zhitnitsky, K.Fukushima, H.J.Warringa et al; photons and vector mesons in Chern-Simons constant background; A.A., D.Espriu, V.A.Andrianov et al.
  - c. **Compact dense star filled by axions?**
- ▶ **Finite volume effects:** passing through and reflecting from a boundary A.A., S.S.Kolevatov, R.Soldati (2011)
- ▶ **Quantization:** Bogoliubov transformation from vacuum to parity breaking medium and back.

## Massive MCS electrodynamics (CFJ model)

$$\mathcal{L}_{MCS} = -\frac{1}{4} F^{\alpha\beta}(x) F_{\alpha\beta}(x) + \frac{1}{2} m^2 A_\nu(x) A^\nu(x) + \frac{1}{2} \zeta_\mu A_\nu(x) \tilde{F}^{\mu\nu}(x) + \text{g.f.}$$

In momentum space wave Eqs.

$$\begin{cases} [g^{\lambda\nu} (k^2 - m^2) - k^\lambda k^\nu + i \varepsilon^{\lambda\nu\alpha\beta} \zeta_\alpha k_\beta] \mathbf{a}_\lambda(k) = 0 \\ k^\lambda \mathbf{a}_\lambda(k) = 0 \end{cases}$$

Projection onto different polarizations with the help of

$$S_\lambda^\nu = \delta_\lambda^\nu D + k^\nu k_\lambda \zeta^2 + \zeta^\nu \zeta_\lambda k^2 - \zeta \cdot k (\zeta_\lambda k^\nu + \zeta^\nu k_\lambda); \quad D \equiv (\zeta \cdot k)^2 - \zeta^2 k^2$$

Transversal polarizations,

$$\pi_\pm^{\mu\nu} \equiv \frac{S^{\mu\nu}}{2D} \pm \frac{i}{2} \varepsilon^{\mu\nu\alpha\beta} \zeta_\alpha k_\beta D^{-\frac{1}{2}}; \quad \varepsilon_\pm^\mu(k) = \pi_\pm^{\mu\lambda} \varepsilon_\lambda^{(0)}$$

Scalar and longitudinal polarizations,

$$\varepsilon_S^\mu(k) \equiv \frac{k^\mu}{\sqrt{k^2}}, \quad \varepsilon_L^\mu(k) \equiv (D k^2)^{-\frac{1}{2}} (k^2 \zeta^\mu - k^\mu \zeta \cdot k)$$

# Energy spectrum and birefringence

Transversal polarizations,

$$K_{\nu}^{\mu} \varepsilon_{\pm}^{\nu}(k) = (k^2 - m^2 \pm \sqrt{D}) \varepsilon_{\pm}^{\mu}(k);$$
$$\omega_{\mathbf{k}, \pm} = \begin{cases} \sqrt{\mathbf{k}^2 + m^2 \pm \zeta_0 |\mathbf{k}|}; & \zeta_{\mu} = (\zeta_0, 0, 0, 0) \\ \sqrt{\mathbf{k}^2 + m^2 + \frac{1}{2}\zeta_x^2 \pm \zeta_x \sqrt{k_1^2 + m^2 + \frac{1}{4}\zeta_x^2}} & \zeta_{\mu} = (0, -\zeta_x, 0, 0) \end{cases}$$

**CFJ model - massless photons:** in observations of very remote radio galaxies left-handed and right-handed circular e.m. waves propagate with different velocities. **Birefringence!**

Polarizations of linearly polarized radio waves could be rotated with distance  $L$ !

$$\zeta_0 \ll |\mathbf{k}| \quad k_{\pm} \simeq \omega_{\mathbf{k}} \mp \frac{1}{2}\zeta_0; \quad \Delta\phi_{rotation} = \frac{1}{2}(\phi_L - \phi_R) = \frac{1}{2}\zeta L.$$

Distances are of order the Hubble scale  $\sim 10^{10}$  l.y. and from the analysis of 160 galaxies with linearly polarized radio waves  $\Rightarrow |\zeta| < 10^{-33} \text{eV} \sim 1/R_{Universe}$

**Large-scale Universe is not birefringent! (at low energies)**

## Motivation of local PB

Parity: well established global symmetry of strong interactions. Reasons to believe it may be broken in a finite volume?!

- ▶ **quantum fluctuations of  $\theta$  parameter** ( $P$ -odd bubbles [T. D. Lee and G. C. Wick ...]: their manifestation in Chiral Magnetic Effect (CME))[D. E. Kharzeev, L. D. McLerran, A.Zhitnitsky, K.Fukushima, H. J. Warringa]

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- ▶ *Our special interest:*  
**PB background inside a hot dense nuclear fireball in HIC !?**



## Topological charge

$$T_5(t) = \frac{1}{8\pi^2} \int_{\text{vol.}} d^3x \varepsilon_{jkl} \text{Tr} \left( G^j \partial^k G^l - i \frac{2}{3} G^j G^k G^l \right)$$

in a finite volume it may arise from quantum fluctuations in hot QCD medium

(due to sphaleron transitions!? [Manton, Rubakov, Shaposhnikov, McLerran])

and survive for a sizeable lifetime in a heavy-ion fireball,

$$\langle \Delta T_5 \rangle \neq 0 \quad \text{for} \quad \Delta t \simeq \tau_{\text{fireball}} \simeq 5 - 10 \text{ fm},$$

For this period one can control the value of  $\langle \Delta T_5 \rangle$  introducing into the QCD Lagrangian a topological chemical potential

$$\Delta L = \mu_\theta \Delta T_5, \quad \Delta T_5 = T_5(t_f) - T_5(0) = \frac{1}{8\pi^2} \int_0^{t_f} \int_{\text{vol.}} d^3x \text{Tr} \left( G^{\mu\nu} \tilde{G}_{\mu\nu} \right)$$

in a gauge invariant way.

## Axial baryon charge

Partial conservation of isosinglet axial current broken by gluon anomaly (consider the light quarks only),

$$\partial_\mu J_5^\mu - 2im_q J_5 = \frac{N_f}{8\pi^2} \text{Tr} \left( G^{\mu\nu} \tilde{G}_{\mu\nu} \right)$$

predicts the induced **chiral (axial) charge**

$$\frac{d}{dt} (Q_5^q - 2N_f T_5) \simeq 0, \quad m_q \simeq 0, \quad Q_5^q = \int_{\text{vol.}} d^3x \bar{q} \gamma_0 \gamma_5 q = \langle \underline{N_L - N_R} \rangle$$

to be conserved  $\dot{Q}_5^q \simeq 0$  (in the chiral limit  $m_q \simeq 0$ ) during  $\tau_{\text{fireball}}$ .

## Axial chemical potential

Axial chemical potential can be associated with approximately conserved  $Q_5^q$  (for  $u, d$  quarks!)

$$\Delta L_q = \mu_5^q Q_5^q,$$

to reproduce a corresponding

$$\langle \Delta T_5 \rangle \simeq \frac{1}{2N_f} \langle Q_5^q \rangle, \iff \mu_5^q \simeq \frac{1}{2N_f} \mu_\theta$$

LPB to be investigated in e.m. interactions of leptons and photons with hot/dense nuclear matter via heavy ion collisions.

- ▶ e.m. interaction implies

$$Q_5^q \rightarrow \tilde{Q}_5 = Q_5^q - T_5^{\text{em}}, \quad T_5^{\text{em}} = \frac{1}{16\pi^2} \int_{\text{vol.}} d^3x \epsilon_{jkl} A^j \partial^k A^l$$

- ▶  $\mu_5$  is conjugated to (nearly) conserved  $\tilde{Q}_5$

# Axial chemical potential in hadron Lagrangians

**Bosonization** of  $Q_5^q$  following VMD prescription

$$\mathcal{L}_{\text{int}} = \bar{q}\gamma_\mu \hat{V}^\mu q; \quad \hat{V}_\mu \equiv -eA_\mu Q + \frac{1}{2}g_\omega\omega_\mu \mathbb{I} + \frac{1}{2}g_\rho\rho_\mu^0\tau_3,$$

$$(V_{\mu,a}) \equiv (A_\mu, \omega_\mu, \rho_\mu^0, \phi_\mu), \quad g_\omega \simeq g_\rho \equiv g \simeq 6$$

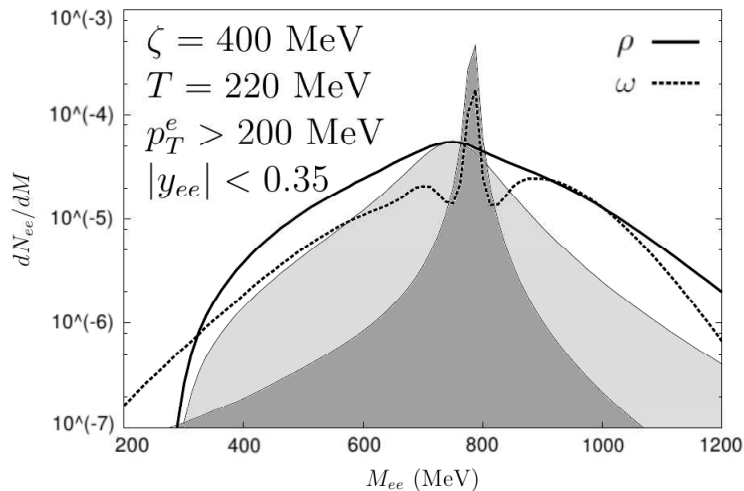
$$\mathcal{L}_{\text{kin}} = -\frac{1}{4}(F_{\mu\nu}F^{\mu\nu} + \omega_{\mu\nu}\omega^{\mu\nu} + \rho_{\mu\nu}\rho^{\mu\nu} + \phi_{\mu\nu}\phi^{\mu\nu}) + \frac{1}{2}V_{\mu,a}(\hat{m}^2)_{a,b}V_b^\mu$$

**$P$ -odd interaction**

$$\mathcal{L}_{\text{mix}} \propto -\frac{1}{4}\varepsilon^{\mu\nu\rho\sigma}\text{Tr}\left[\hat{\zeta}_\mu V_\nu V_{\rho\sigma}\right] = \frac{1}{2}\text{Tr}\left(\hat{\zeta}\varepsilon_{jkl}\hat{V}_j\partial_k\hat{V}_l\right) = \frac{1}{2}\zeta\varepsilon_{jkl}V_{j,a}N_{ab}\partial_k V_{l,b}$$

with  $\hat{\zeta}_\mu = \hat{\zeta}\delta_{\mu 0}$ , spatially homogeneous and isotropic background.

# Resonance splitting in polarizations (corrected for PHENIX acceptance)



# Finite volume: passing through boundary

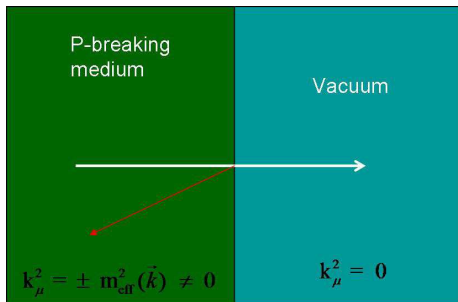
A.A., S.Kolevatov, R.Soldati, JHEP 11 (2011) 007

Mean free paths for vector mesons:

- ▶  $L_\rho \sim 0.8fm$   
 $\ll L_{fireball} \sim 5 - 10fm$
- ▶  $L_\omega \sim 16fm \gg L_{fireball}$   
Why it is relevant in medium?  
(PHENIX confirms!)

LPB "vacuum"  
 $\neq$  empty vacuum  
= coherent state  
of vacuum mesons

Matching on  $\zeta \cdot x = 0$



Thus to save energy-momentum conservation transmission must be accompanied by reflection back. Enhancement of in-medium decays of  $\omega$  mesons!

# MCS electrodynamics in a half space

A possible gauge-invariant choice,

$$-\frac{1}{4} F^{\mu\nu}(x) \tilde{F}_{\mu\nu}(x) \zeta_\lambda x^\lambda \theta(-\zeta \cdot x) \Rightarrow \frac{1}{2} \zeta_\mu A_\nu(x) \tilde{F}^{\mu\nu}(x) \theta(-\zeta \cdot x),$$

which however associates a space-like boundary with a space-like CS vector  $(\zeta_\mu)(x) = \zeta(0, \vec{a})\theta(-\vec{a} \cdot \vec{x})$ ,  $|\vec{a}| = 1$ .

**Compact dense stars filled by axions with density degrading to their surface?!**

Another choice: time-like CS vector and space-like boundary  $(\zeta_\mu)(x) = \zeta(\theta(-\vec{a} \cdot \vec{x}), -\vec{a}x_0\delta(-\vec{a} \cdot \vec{x}))$  gauge invariance condition  $\partial_\nu \zeta_\mu = \partial_\mu \zeta_\nu$ . Singular interaction on a space-like boundary!

**Axial chemical potential for a fireball**

★ ★ ★ ★ ★ ★

**Matching on the boundary**  $\zeta \cdot x = 0$

$$\delta(\zeta \cdot x) [A_{\text{vacuum}}^\mu(x) - A_{\text{MCS}}^\mu(x)] = 0,$$

## Classical solutions

Spatial Chern-Simons vector  $\zeta_\mu = (0, -\zeta_x, 0, 0)$  and orthogonal planes  
 $\hat{k} = (\omega, k_2, k_3)$ ,  $\hat{x} = (x_0, x_2, x_3)$

In the entire space,

$$A_1 = \int \frac{d^3 \hat{k}}{(2\pi)^3} \theta(\omega^2 - k_\perp^2 - m^2) (\tilde{u}_{1\rightarrow}(\omega, k_2, k_3) e^{ik_{10}x_1} + \tilde{u}_{1\leftarrow}(\omega, k_2, k_3) e^{-ik_{10}x_1}) e^{i\hat{k}\hat{x}}$$

**where**  $k_{10}^2 = \omega^2 - m^2 - k_\perp^2$ ,  $k_\perp^2 = k_2^2 + k_3^2$

Two solutions for other components in the different half-spaces taken both on entire axis.

For  $x_1 > 0$  ( $\nu = 0, 2, 3$ )

$$A_\nu = \int \frac{d^3 \hat{k}}{(2\pi)^3} \theta(\omega^2 - k_\perp^2 - m^2) (\tilde{u}_{\nu\rightarrow}(\omega, k_2, k_3) e^{ik_{10}x_1} + \tilde{u}_{\nu\leftarrow}(\omega, k_2, k_3) e^{-ik_{10}x_1}) e^{i\hat{k}\hat{x}}$$

Arrows  $\rightarrow, \leftarrow$  for directions of particle propagation.

For  $x_1 < 0$  ( $A = L, \pm$  eigenstates of suitable polarizations)

$$\tilde{A}_\nu = \sum_A [\tilde{v}_{\nu A\rightarrow}(k_2, k_3, \omega) \delta(k_1 - k_{1A}) + \tilde{v}_{\nu A\leftarrow}(k_2, k_3, \omega) \delta(k_1 + k_{1A})]$$



## MCS dispersion laws and polarizations

The MCS dispersion laws for different polarizations,

$$\left\{ \begin{array}{l} k_{1L} = k_{10} = \sqrt{\omega^2 - m^2 - k_{\perp}^2} \\ k_{1+} = \sqrt{\omega^2 - m^2 - k_{\perp}^2 + \zeta_x \sqrt{\omega^2 - k_{\perp}^2}} \\ k_{1-} = \sqrt{\omega^2 - m^2 - k_{\perp}^2 - \zeta_x \sqrt{\omega^2 - k_{\perp}^2}} \end{array} \right.$$

## Matching on boundary

Matching,

$$\left\{ \begin{array}{l} -k_{10}^2 \left( -\frac{\tilde{u}_{0\rightarrow} - \tilde{u}_{0\leftarrow}}{ik_{10}} + \sum_A \frac{\tilde{v}_{0A\rightarrow} - \tilde{v}_{0A\leftarrow}}{ik_{1A}} \right) = i\zeta_x \left( k_2 \sum_A \frac{\tilde{v}_{3A\rightarrow} - \tilde{v}_{3A\leftarrow}}{ik_{1A}} - k_3 \sum_A \frac{\tilde{v}_{2A\rightarrow} - \tilde{v}_{2A\leftarrow}}{ik_{1A}} \right) \\ -k_{10}^2 \left( -\frac{\tilde{u}_{2\rightarrow} - \tilde{u}_{2\leftarrow}}{ik_{10}} + \sum_A \frac{\tilde{v}_{2A\rightarrow} - \tilde{v}_{2A\leftarrow}}{ik_{1A}} \right) = -i\zeta_x \left( k_3 \sum_A \frac{\tilde{v}_{0A\rightarrow} - \tilde{v}_{0A\leftarrow}}{ik_{1A}} + \omega \sum_A \frac{\tilde{v}_{3A\rightarrow} - \tilde{v}_{3A\leftarrow}}{ik_{1A}} \right) \\ -k_{10}^2 \left( -\frac{\tilde{u}_{3\rightarrow} - \tilde{u}_{3\leftarrow}}{ik_{10}} + \sum_A \frac{\tilde{v}_{3A\rightarrow} - \tilde{v}_{3A\leftarrow}}{ik_{1A}} \right) = i\zeta_x \left( \omega \sum_A \frac{\tilde{v}_{2A\rightarrow} - \tilde{v}_{2A\leftarrow}}{ik_{1A}} + k_2 \sum_A \frac{\tilde{v}_{0A\rightarrow} - \tilde{v}_{0A\leftarrow}}{ik_{1A}} \right) \end{array} \right.$$

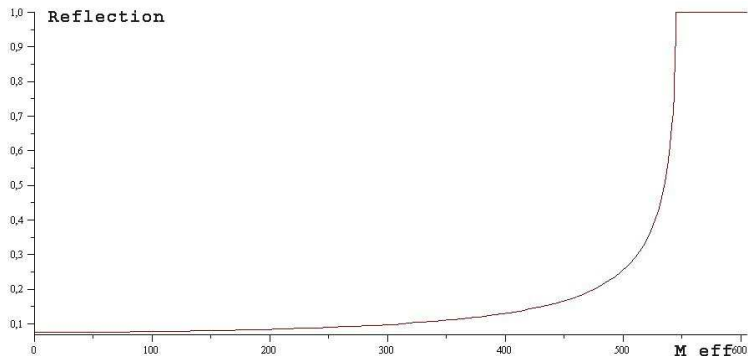
Continuity of  $A$ ,

$$\begin{aligned} \tilde{u}_{\nu\rightarrow}^{(L)} + \tilde{u}_{\nu\leftarrow}^{(L)} &= \tilde{v}_{\nu L\rightarrow} + \tilde{v}_{\nu L\leftarrow} \\ \tilde{u}_{\nu\rightarrow}^{(+)} + \tilde{u}_{\nu\leftarrow}^{(+)} &= \tilde{v}_{\nu+\rightarrow} + \tilde{v}_{\nu+\leftarrow} \\ \tilde{u}_{\nu\rightarrow}^{(-)} + \tilde{u}_{\nu\leftarrow}^{(-)} &= \tilde{v}_{\nu-\rightarrow} + \tilde{v}_{\nu-\leftarrow} \end{aligned}$$

### Final relations

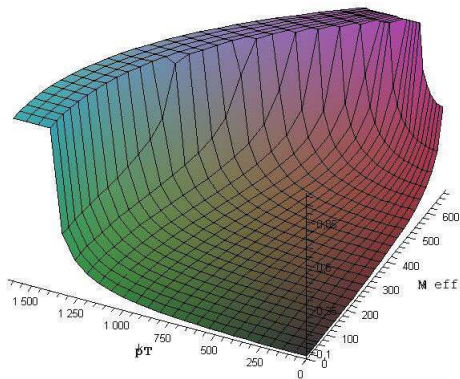
$$\begin{aligned} \tilde{u}_{\nu\rightarrow}^{(A)} &= \frac{1}{2} \left( \tilde{v}_{\nu A\rightarrow} \left( \frac{k_{1A} + k_{10}}{k_{10}} \right) - \tilde{v}_{\nu A\leftarrow} \left( \frac{k_{1A} - k_{10}}{k_{10}} \right) \right) \\ \tilde{u}_{\nu\leftarrow}^{(A)} &= \frac{1}{2} \left( -\tilde{v}_{\nu A\rightarrow} \left( \frac{k_{1A} - k_{10}}{k_{10}} \right) + \tilde{v}_{\nu A\leftarrow} \left( \frac{k_{1A} + k_{10}}{k_{10}} \right) \right) \end{aligned}$$

# Reflection from boundary depending on effective mass: negative chirality

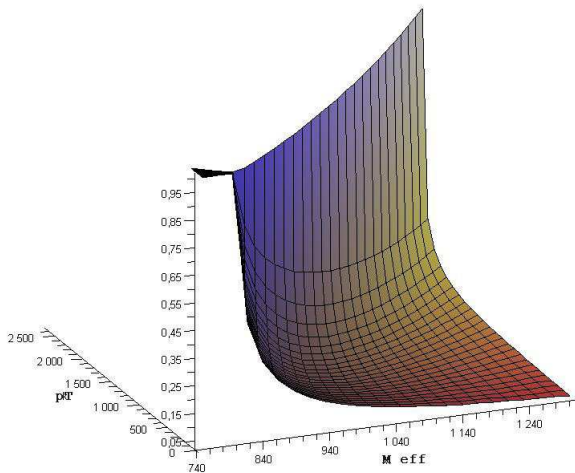


Dependence on effective mass for zero  $p_T$ , CS vector  $\zeta = 400$  MeV

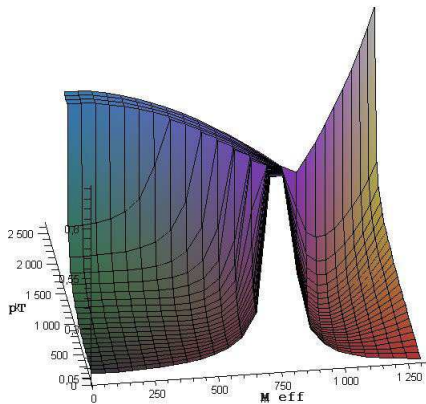
# Reflection from boundary: negative chirality, $\rho_T \neq 0$



# Reflection from boundary: positive chirality, $p_T \neq 0$



# Reflection from boundary: both chiralities, $\rho_T \neq 0$



# Quantization of MCS in a half-space: Bogolyubov transformation

In vacuum,

$$A_{\text{vacuum}}^{\mu}(x) = \int d^3\hat{k} \theta(\omega^2 - k_{\perp}^2 - m^2) \sum_{r=1}^3 \left[ \mathbf{a}_{\hat{k},r} u_{\hat{k},r}^{\mu}(x) + \mathbf{a}_{\hat{k},r}^{\dagger} u_{\hat{k},r}^{\mu,*}(x) \right],$$

Canonical commutation relations  $[\mathbf{a}_{\hat{k},r}, \mathbf{a}_{\hat{k}',s}^{\dagger}] = \delta(\hat{k} - \hat{k}') \delta_{rs}$

In P-breaking medium ( $A \in \{L, +, -\}$ ),

$$A_{\text{MCS}}^{\nu}(x) = \int d^3\hat{k} \theta(\omega^2 - k_{\perp}^2 - m^2) \sum_A \left[ c_{\hat{k},A} v_{\hat{k},A}^{\nu}(x) + c_{\hat{k},A}^{\dagger} v_{\hat{k},A}^{\nu,*}(x) \right]$$

Canonical commutation relations,  $[c_{\hat{k},A}, c_{\hat{k}',A'}^{\dagger}] = -g_{AA'} \delta(\hat{k} - \hat{k}')$

Matching,

$$v_{\hat{k},A}^{\nu}(\hat{x}) = \sum_{s=1}^3 \left[ \alpha_{sA}(\hat{k}) u_{\hat{k},s}^{\nu}(\hat{x}) - \beta_{sA}(\hat{k}) u_{\hat{k},s}^{\nu,*}(\hat{x}) \right]$$

## Bogoliubov transformation

$$\mathbf{a}_{\hat{k},r} = \sum_{A=\pm,L} \left[ \alpha_{rA}(\hat{k}) c_{\hat{k},A} - \beta_{rA}^*(\hat{k}) c_{\hat{k},A}^{\dagger} \right] \quad c_{\hat{k},A} = \sum_{r=1}^3 \left[ \alpha_{Ar}^*(\hat{k}) \mathbf{a}_{\hat{k},r} + \beta_{Ar}^*(\hat{k}) \mathbf{a}_{\hat{k},r}^{\dagger} \right]$$

## Vacuums as coherent states

Two different Fock vacua

$$\mathbf{a}_{\hat{k},r}|0\rangle = 0 \quad \mathbf{c}_{\hat{k},A}|\Omega\rangle = 0$$

From Bogoliubov transformation,

$$|0\rangle = \mathcal{N} \exp \left[ \int d^3\hat{k} \theta(\omega^2 - k_{\perp}^2 - m^2) \times \right. \\ \left. \times \left\{ \frac{\beta_{r+}^*(\hat{k})}{2\alpha_{r+}(\hat{k})} (\mathbf{c}_{\hat{k},+}^{\dagger})^2 + \frac{\beta_{r-}^*(\hat{k})}{2\alpha_{r-}(\hat{k})} (\mathbf{c}_{\hat{k},-}^{\dagger})^2 + \frac{\beta_{rL}^*(\hat{k})}{2\alpha_{rL}(\hat{k})} (\mathbf{c}_{\hat{k},L}^{\dagger})^2 \right\} \right] |\Omega\rangle$$

and inversely

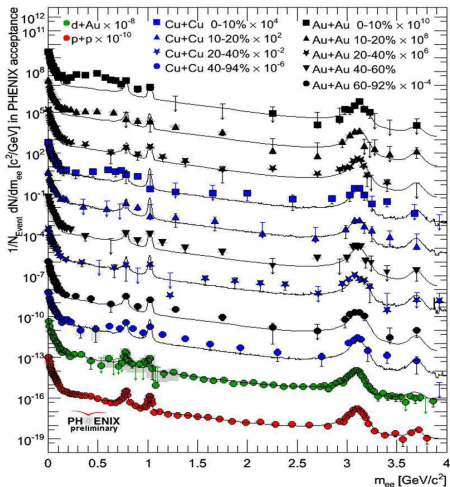
$$|\Omega\rangle = \tilde{\mathcal{N}} \exp \left[ \int d^3\hat{k} \theta(\omega^2 - k_{\perp}^2 - m^2) \times \right. \\ \left. \times \left\{ \frac{-\beta_{A1}^*(\hat{k})}{2\alpha_{A1}^*(\hat{k})} (\mathbf{a}_{\hat{k},1}^{\dagger})^2 + \frac{-\beta_{A2}^*(\hat{k})}{2\alpha_{A2}^*(\hat{k})} (\mathbf{a}_{\hat{k},2}^{\dagger})^2 + \frac{-\beta_{A3}^*(\hat{k})}{2\alpha_{A3}^*(\hat{k})} (\mathbf{a}_{\hat{k},3}^{\dagger})^2 \right\} \right] |0\rangle$$



## Conclusions

- ▶ Local (finite-volume) PB is not forbidden by any physical principle in QCD at finite temperature/density
- ▶ The effect leads to unexpected modifications of the in-medium properties of vector mesons and photons
- ▶ LPB seems to be capable of explaining in a natural way the PHENIX 'anomaly'
- ▶ Boundary enhancement of in-medium  $\omega$  decays + LPB  $\rightarrow$  broadening of  $\omega$  resonance in fireballs (observed on PHENIX!)
- ▶ Axion stars discovery from exotic photon spectra (boundary effects)??

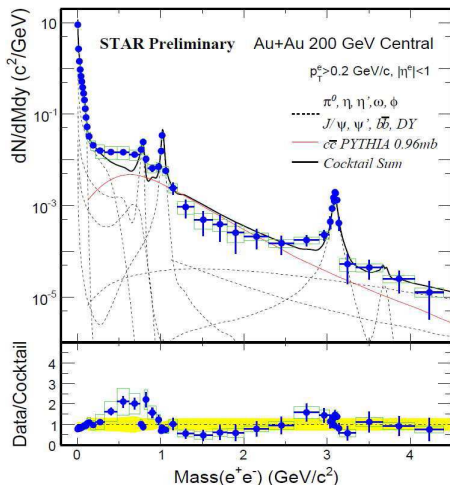
# PHENIX anomaly: abnormal $e^+e^-$ excess in central HIC at low $p_t$



Hint to LPB?

[PHENIX Data Plot (id p1147) 2011]

# STAR anomaly: abnormal $e^+e^-$ excess in central HIC at low $p_t$



Hint to LPB?

[STAR Collaboration, J.Phys.G G38 (2011) 124134]

# Resonance splitting in polarizations (corrected for PHENIX acceptance)

