



Quest for new superconductors

...or superconductivity entering the Iron Age

Igor Mazin, Naval Research Laboratory, Washington D. C.

As coarse as my own wits are, I have been privileged to wear the boots of the Sagacious and be clad in the robes of the Virtuous.

The Supplication of Daniel the Prisoner, a Russian monk, XIII century.


NERL

Physica C 468 (2008) 105–110


www.elsevier.co

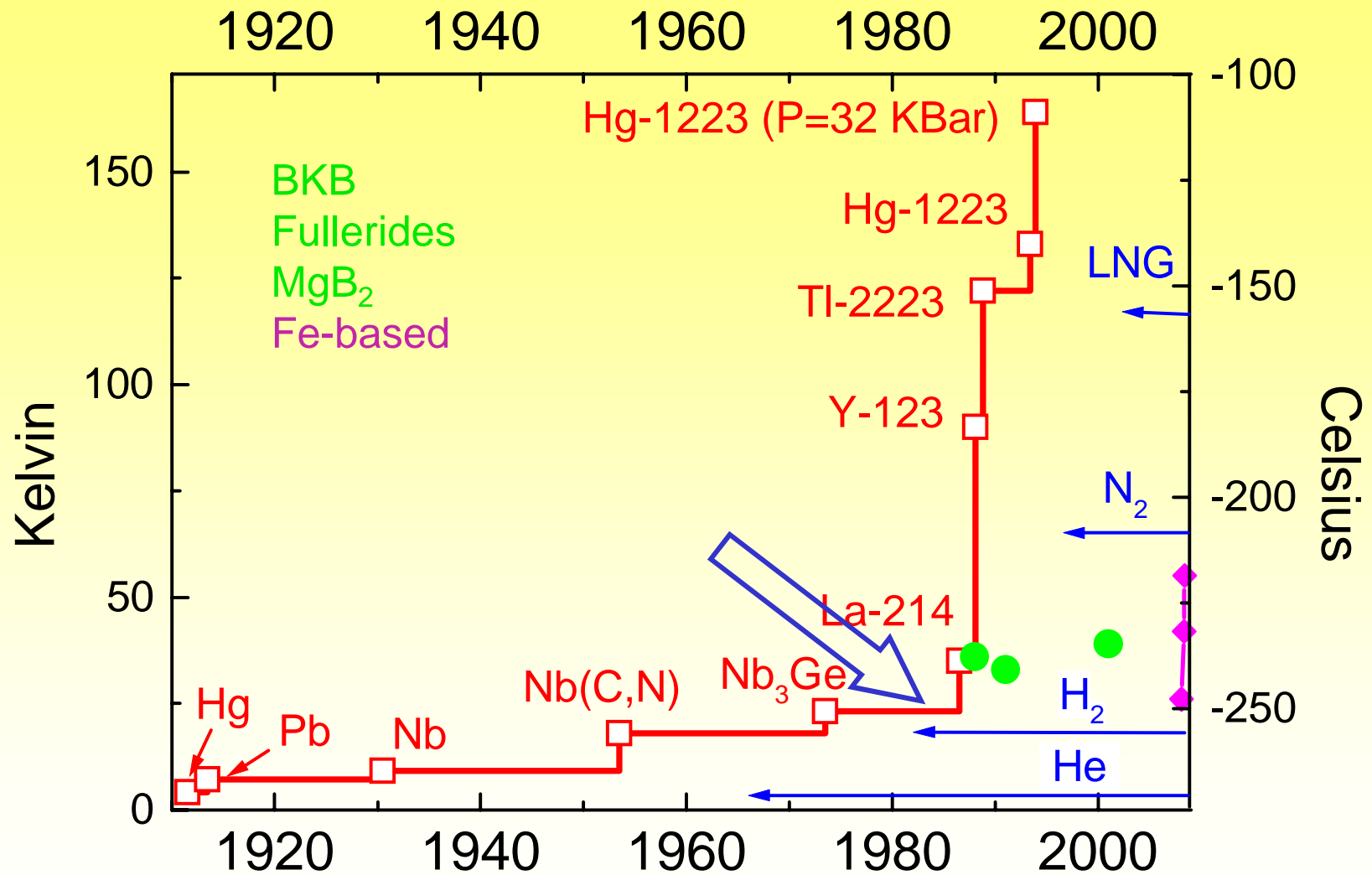
Vitaly Ginzburg and high temperature superconductivity:
Personal reminiscences

Igor I. Mazin *





A brief history of superconductivity





...in search of a theory of primeness...

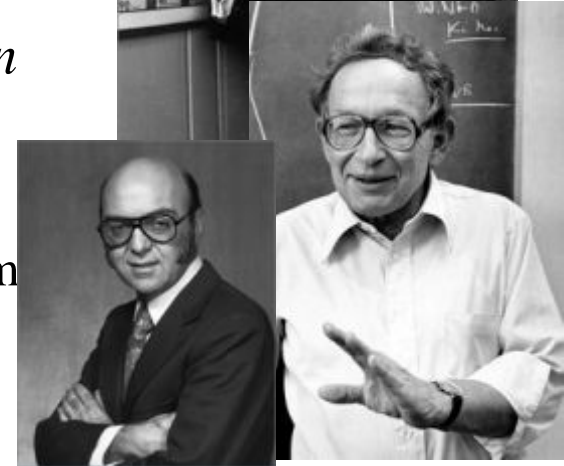
- 1, 3, 5, 7 are all prime. *Ergo*, all odd numbers are prime.
- 9 is not prime! *This is an experimental error. To test this, let us look at more odd numbers:*
- 11 is prime and so is 13. The hypothesis has been confirmed and demonstrated it's predictive power!

Any correct theory of primeness should be able to explain why all odd numbers are prime.

...and any correct theory of s/c must explain why the maximum T_c is limited by 30 K (as of 1985)



...in search of a theory of primeness...



B.T. Matthias, *Science* **144** (1964) 373: *Why has it been relatively easy, within the last 10 years, to reach transition temperatures of 17? to 18?K in many intermetallic systems and impossible to raise this value even by as little as half a degree?*

M.L. Cohen, P.W. Anderson, Comments on the maximum superconducting transition temperature, in: D.H. Douglass (Ed.), *Superconductivity in d- and f-Band Metals*, AIP, New York, 1972

$$T_c \approx \theta \exp\{-1/[\lambda/(1 + \lambda) - \mu^*]\}$$

$$\mu^* = \mu/[1 + \mu \ln(E/\theta)]$$

$$\lambda = \mu$$

$$T_c(\text{max}) = E \exp(-4 - 3/\lambda)$$

$$T_c(\text{max}) \sim 10\text{-}30 \text{ K for } \lambda \sim 1\text{-}2$$

$$E \exp(-3/\lambda)$$

$T_c(\text{max}) \sim 50$ times higher.

OK, let $\lambda(\text{max})$ be $1/2 \dots$



...in search of a theory of primeness...



Timeline

1964:
Matthias
poses his
challenge

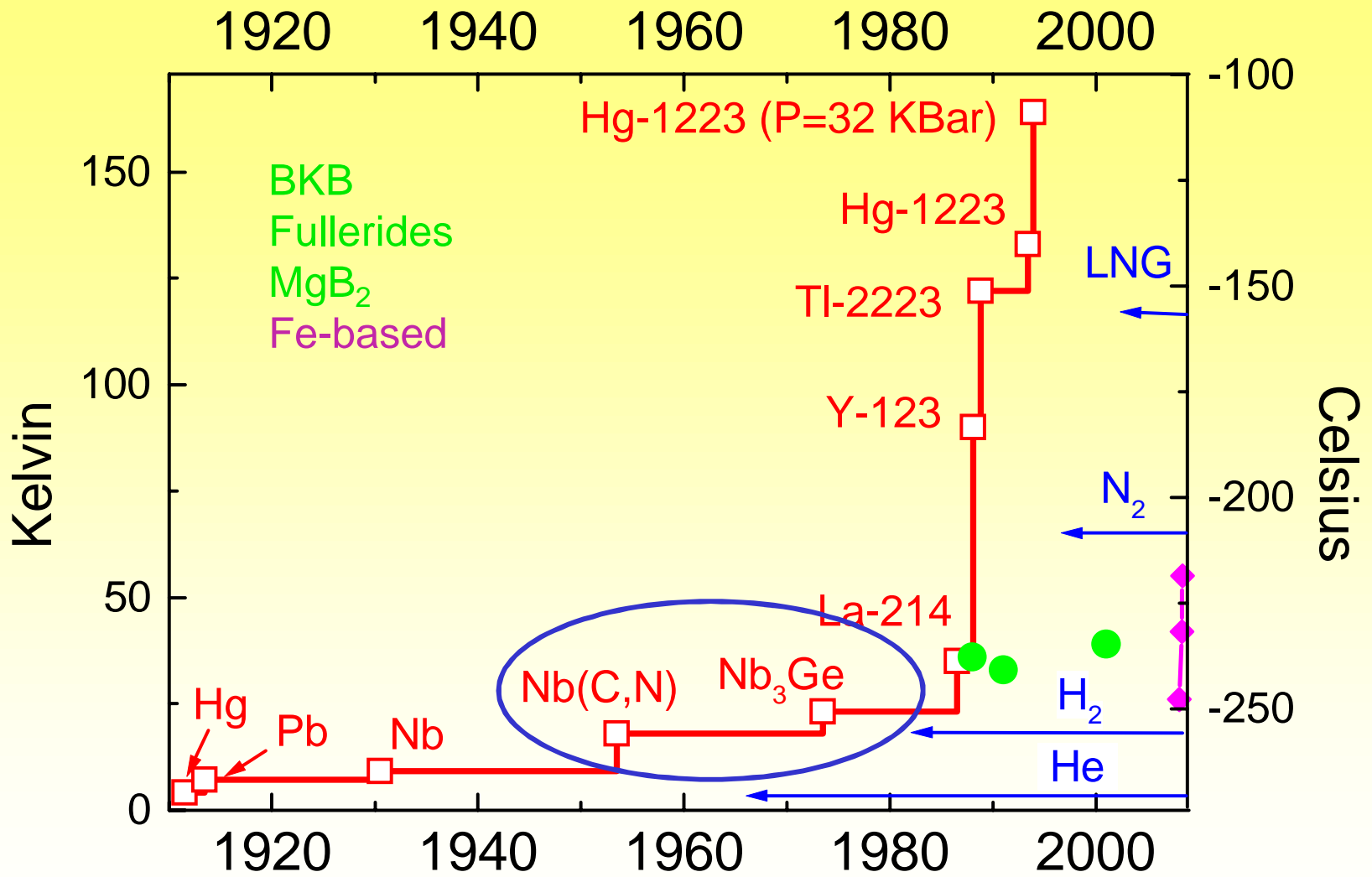
1976: I come
to the V.L.'s
group as a
student

1972:
Anderson
responds

1978-1981:
Dolgov-Kirzhnits-
Maksimov



$$\lambda = \mu$$





Berndt Matthias' rules

Six rules for a successful search for new superconductors

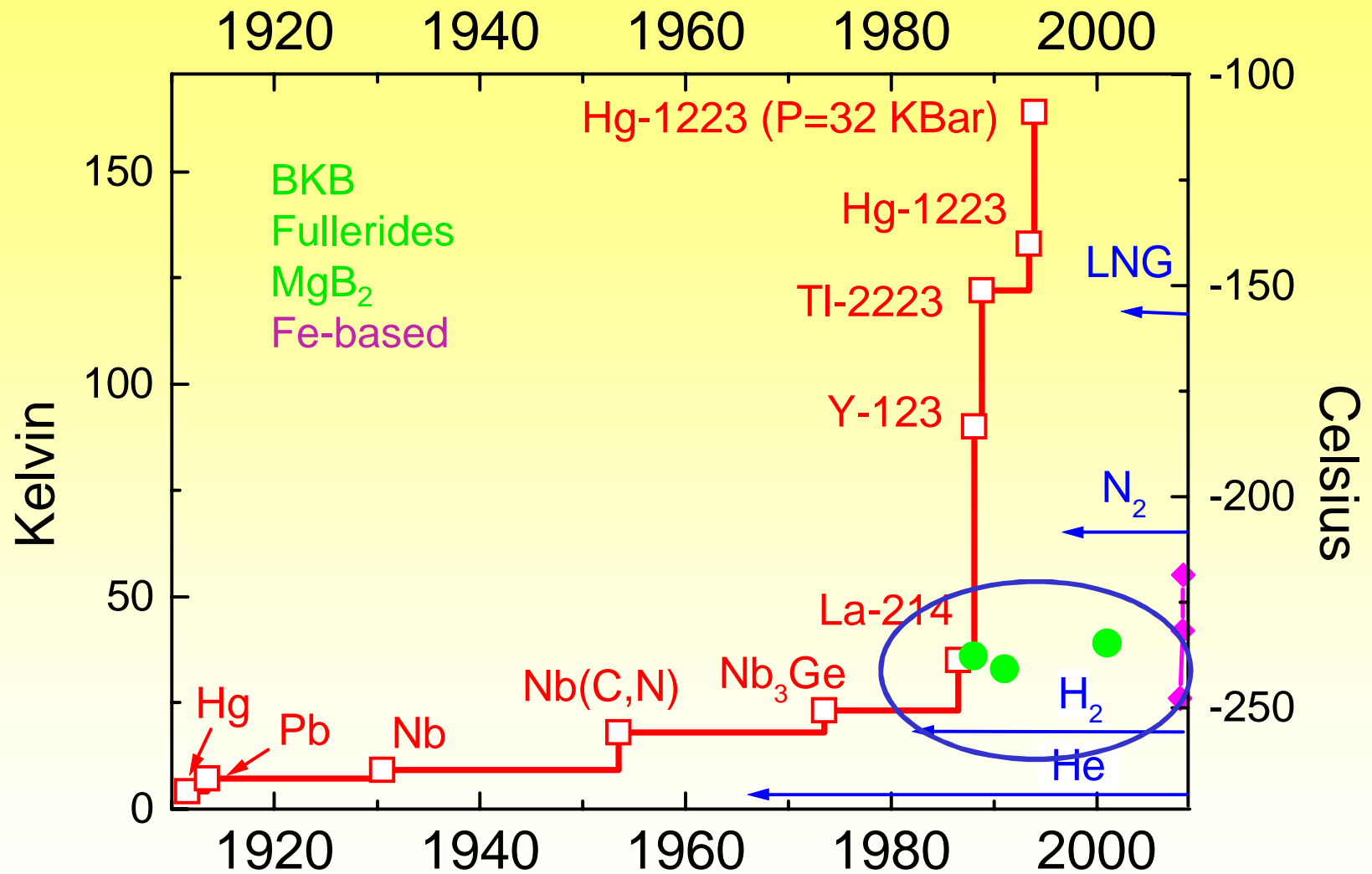
- 1 . A high symmetry is good; cubic symmetry is the best.
2. A high density of electronic states is good.
3. Stay away from oxygen.
4. Stay away from magnetism.
5. Stay away from insulators.
6. Stay away from theorists.



*All these rules
(with possible
exception of #6)
have been proven
wrong in cuprates*



Are cuprates unique?





11000 years ago: Wolf domesticated

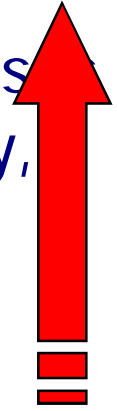
...4000 years... different wolf species domesticated; various dog breeds created and improved



7000 years ago: Goat domesticated

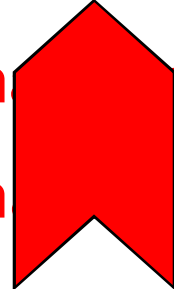


Sheep, cattle, chicken, swine, ass domesticated within, presumably, the next 1000 years.



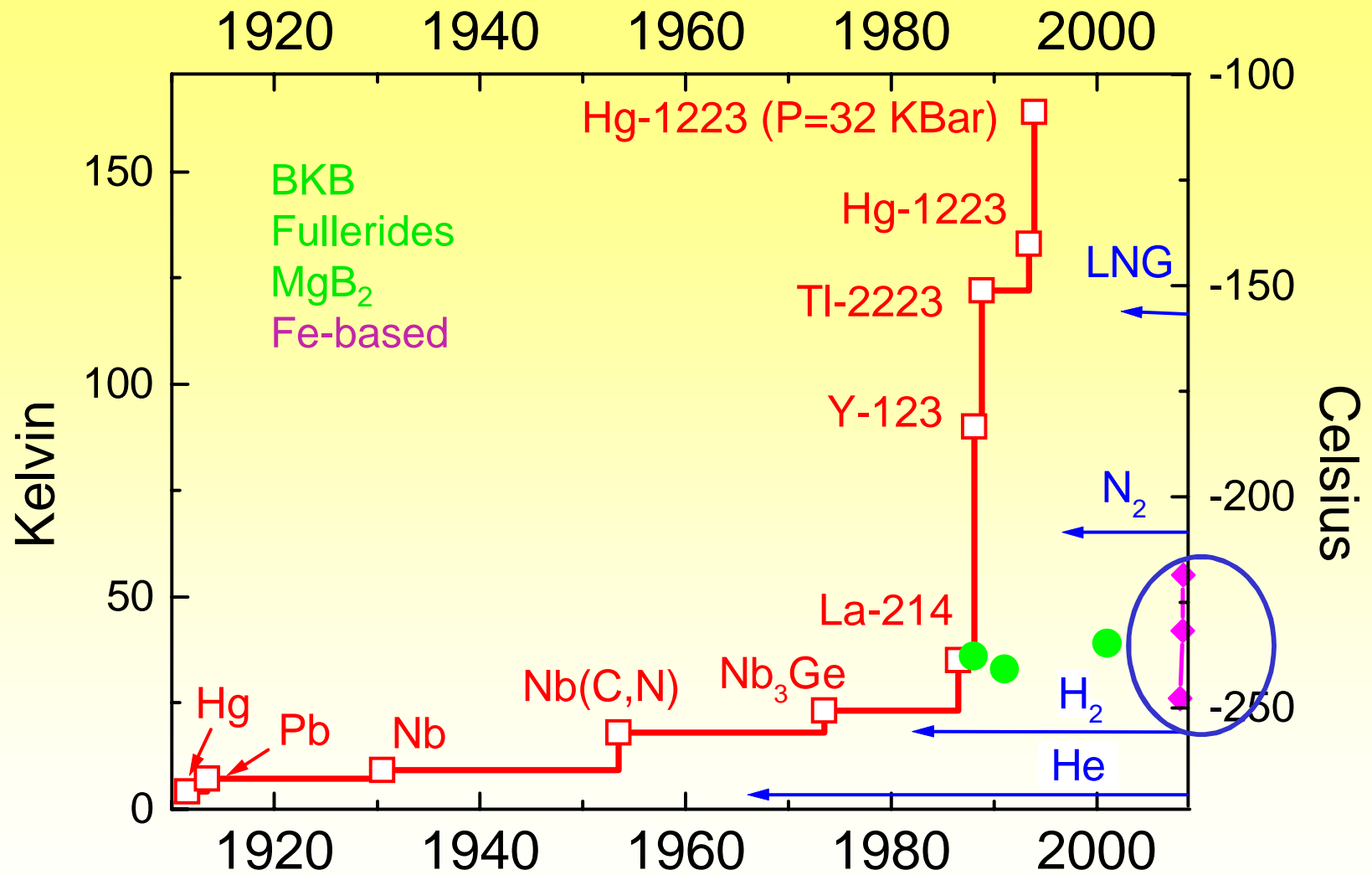
What is our Current Status?

What is our Basic Research Challenge?



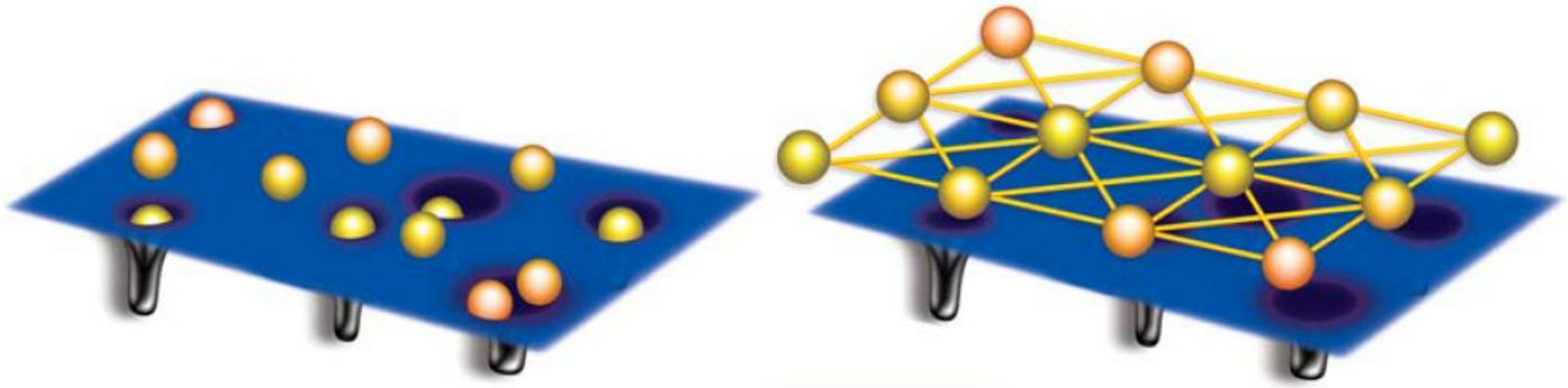


Goat discovered?





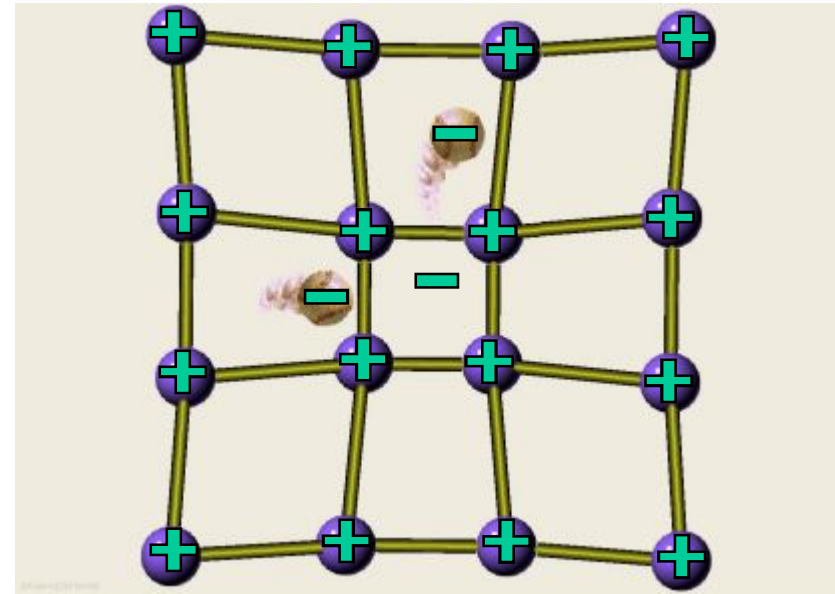
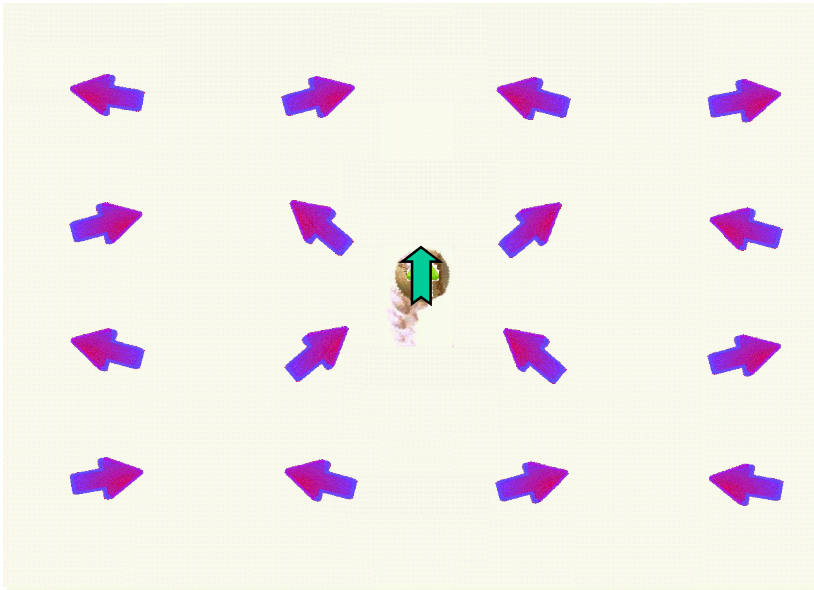
BCS basics



1. **Macroscopically coherent state**
2. **Pairing (to go from the Fermi statistics to the Bose statistics)**
3. **Pairing interaction**
 - *Not necessarily phonons*
 - *Not necessarily attraction*
4. **Excitation gap (robustness)**

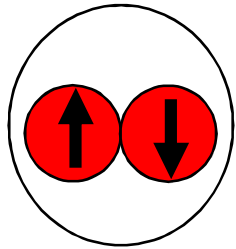


Pairing interaction: phonons vs. spin fluctuations



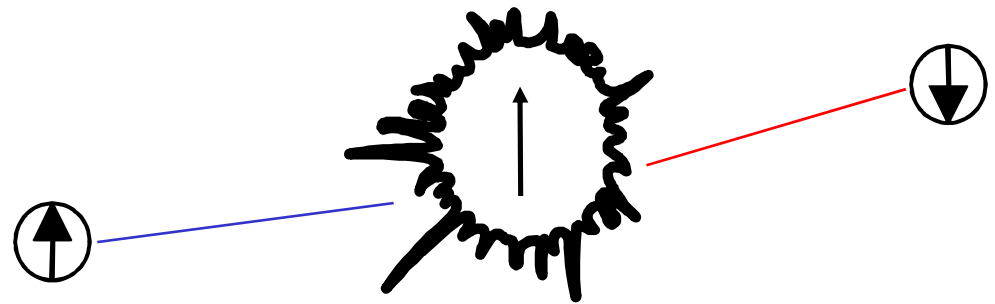
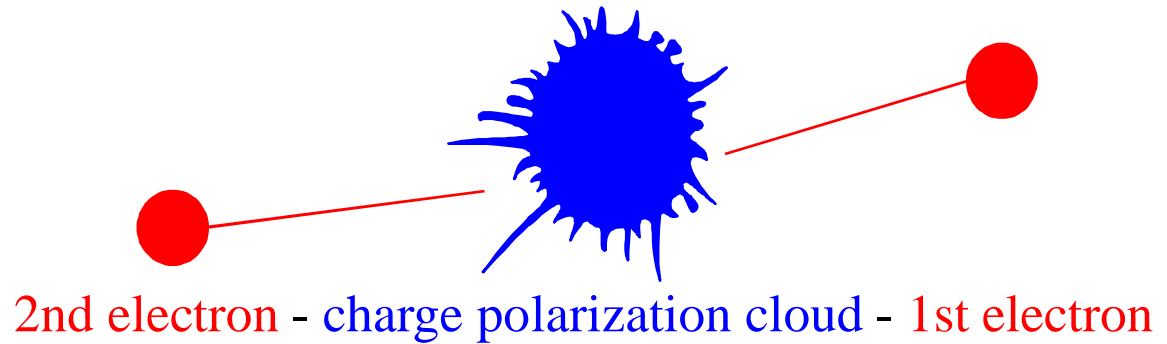


Superconductivity and spin fluctuations



singlet

charge fluctuations
(phonons) mediate
attraction; spin fluctuations
mediate repulsion



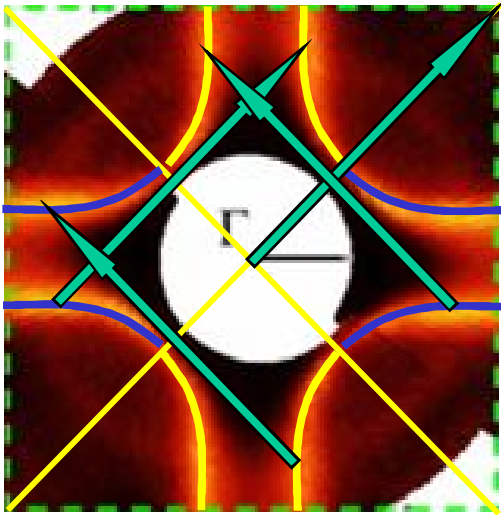
2nd electron - spin polarization cloud - 1st electron

$$\Delta_{\mathbf{k}\alpha} = \sum_{\mathbf{q}\beta} V_{\mathbf{k}\mathbf{q},\alpha\beta} \Delta_{\mathbf{q}\beta} F(\Delta_{\mathbf{q}\beta}, T)$$

If $\Delta_{\alpha\mathbf{k}}$ and $\Delta_{\mathbf{k}\beta}$ have opposite sign, a negative (repulsive) V can still be pairing.



How does it work in high-Tc cuprates?



Fermi surface of BSCCO measured by ARPES
 (http://en.wikipedia.org/wiki/Fermi_surface)

Parent compounds have checkerboard antiferromagnetism. Superexchange interaction is peaked at $Q=(\pi,\pi)$

It is perfectly well matching the fermiology of high-Tc cuprates

There are two ingredients in this recipe: (1) Fermiology

and (2) momentum dependence of spin fluctuations

$$\Delta_{\mathbf{k}\alpha} = \sum_{\mathbf{q}\beta} V_{\mathbf{k}\mathbf{q},\alpha\beta} \Delta_{\mathbf{q}\beta} F(\Delta_{\mathbf{q}\beta}, T)$$

If $\Delta_{\alpha\mathbf{k}}$ and $\Delta_{\beta\mathbf{k}}$ have opposite sign, a negative (repulsive) V can still be pairing.



The cuprates duel: pairing glue – yes or no?

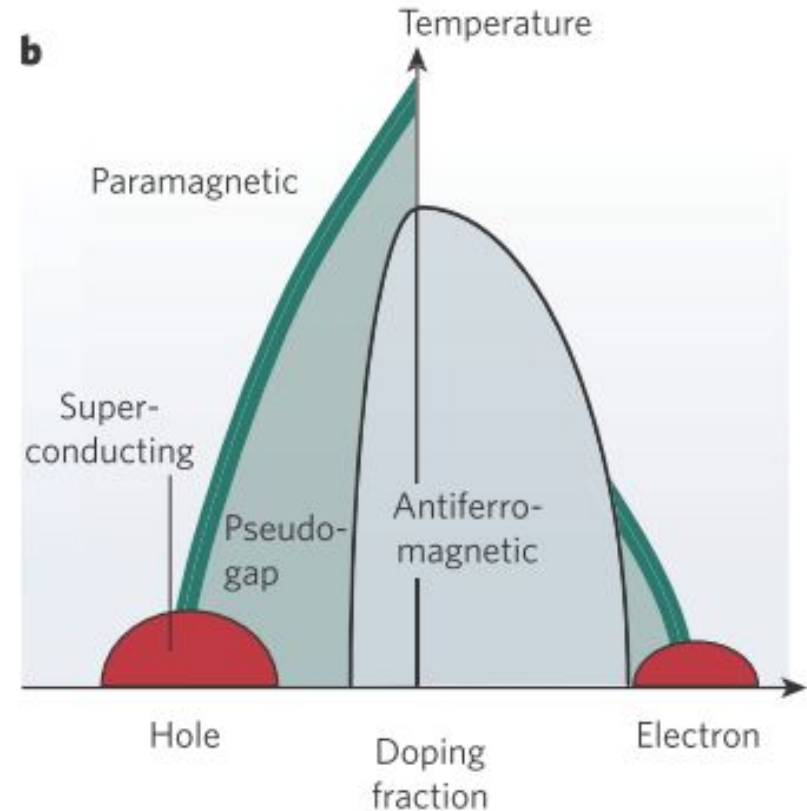
Two schools of thoughts:

1. Pairing glue, most likely magnetic.

- Superconductivity emerges from “outside”, from Fermi liquid.
- Modified Eliashberg theory.
- Proponents: Ginzburg, Maksimov, Pines, Scalapino,...

2. Completely novel mechanisms

- Superconductivity emerges from the Mott-Hubbard state
- Pairing creates energy gain for all electrons (in different ways in different theories).
- Proponents: Anderson (RVB, IPT, ...), Laughlin (Gossamer s/c), ...





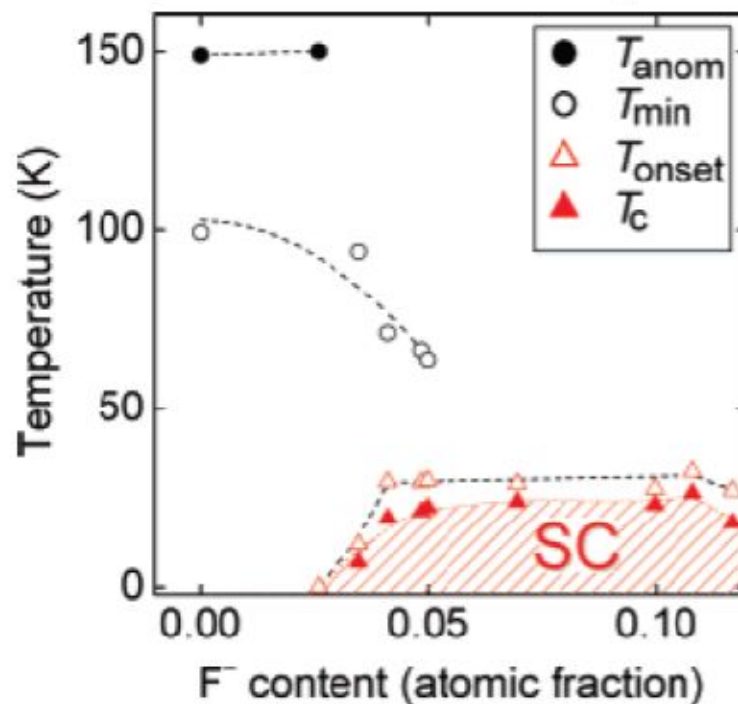
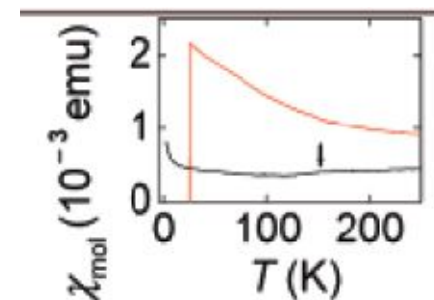
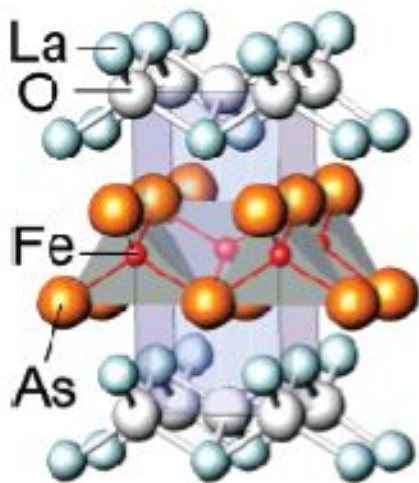
Pairing glue proponents celebrate

J|A|C|S
COMMUNICATIONS

Published on Web 02/23/2008

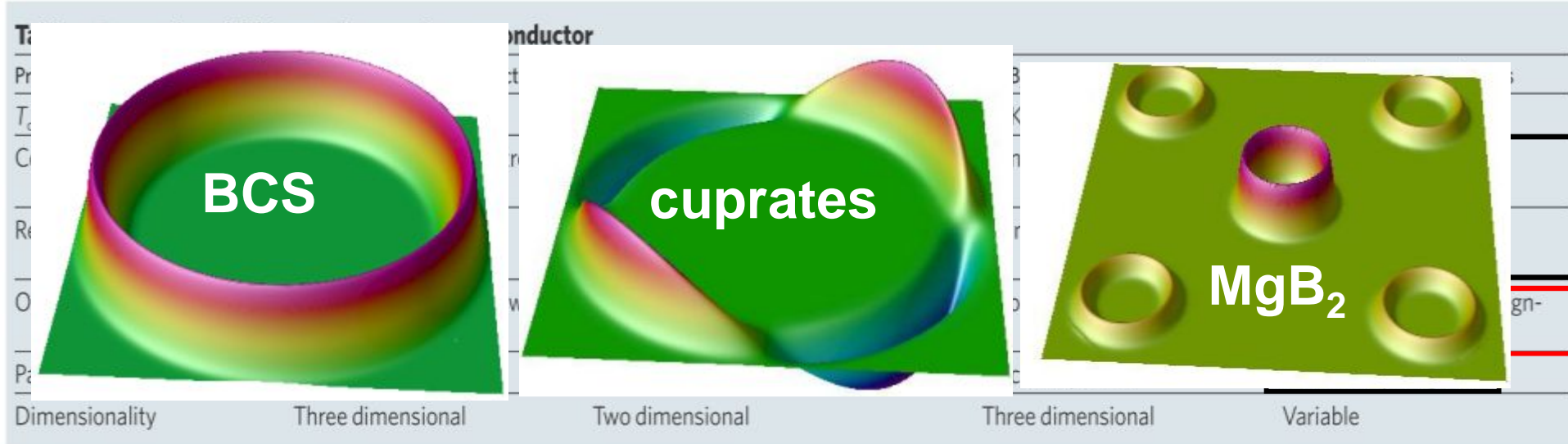
Iron-Based Layered Superconductor $\text{La}[\text{O}_{1-x}\text{F}_x]\text{FeAs}$ ($x = 0.05\text{--}0.12$) with $T_c = 26\text{ K}$ (soon up to 57 K)

Yoichi Kamihara,^{*,†} Takumi Watanabe,[‡] Masahiro Hirano,^{†,§} and Hideo Hosono^{†,‡,§}





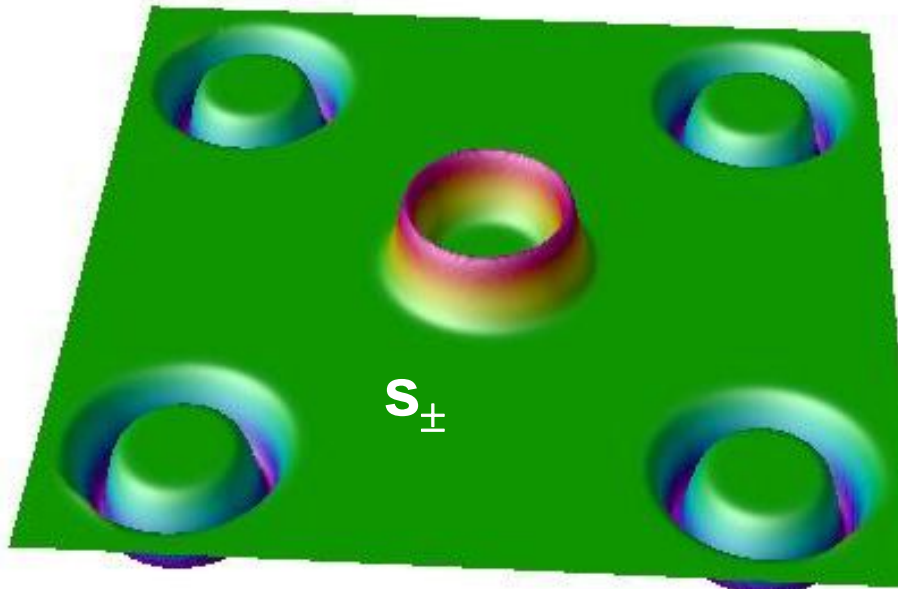
Comparison with other high- T_c materials



From *I. I. A*

Other review
R.L. Green

In some
In many



review).

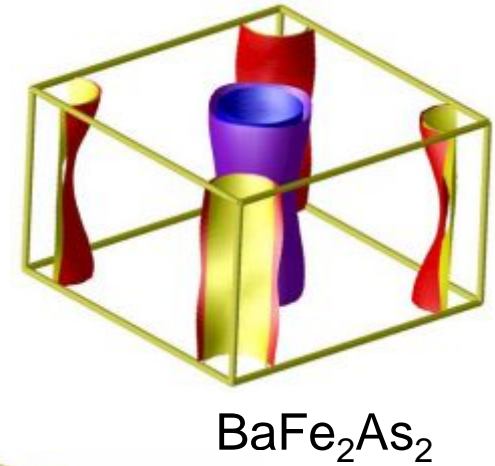
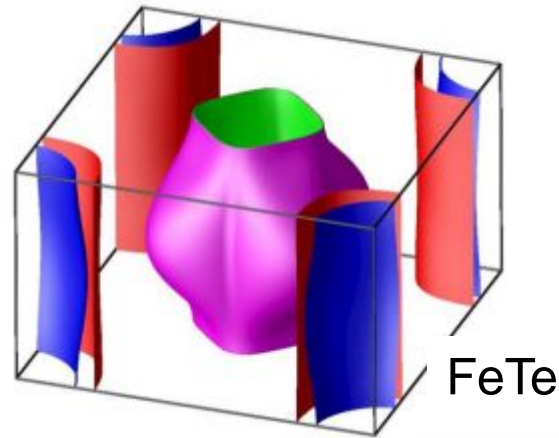
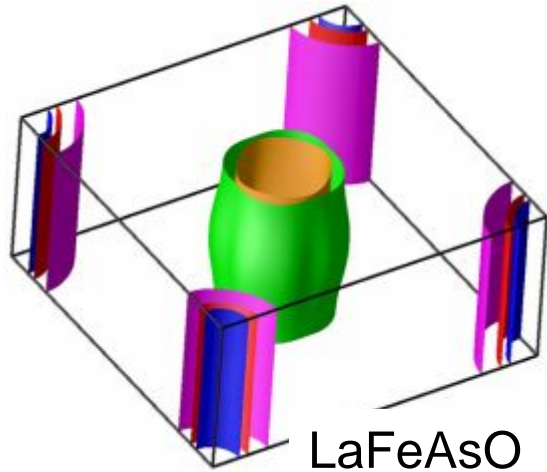
J. Paglione and

469, 614 (2009).

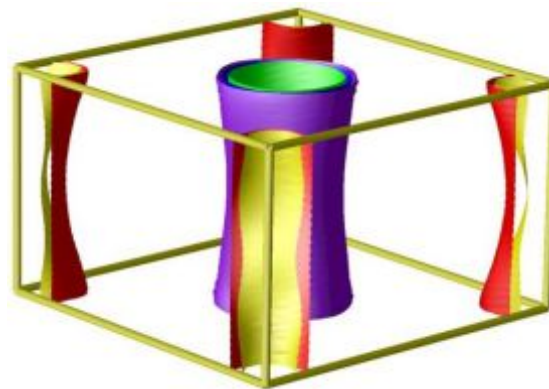
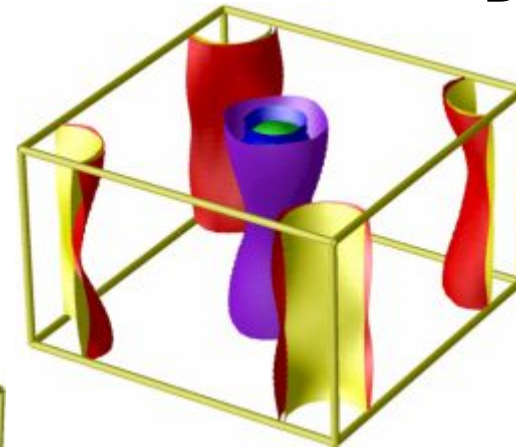
cuprates and MgB_2 .
new paradigm.



Fe-based superconductors: Fermiology



Ba122 – 10%e



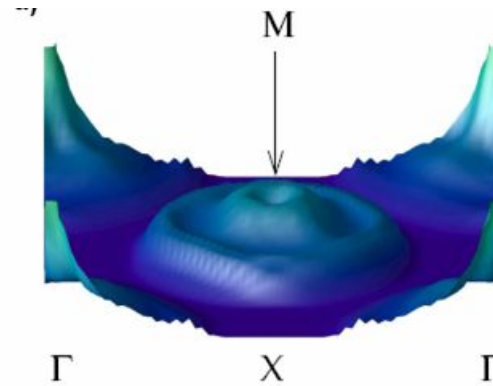
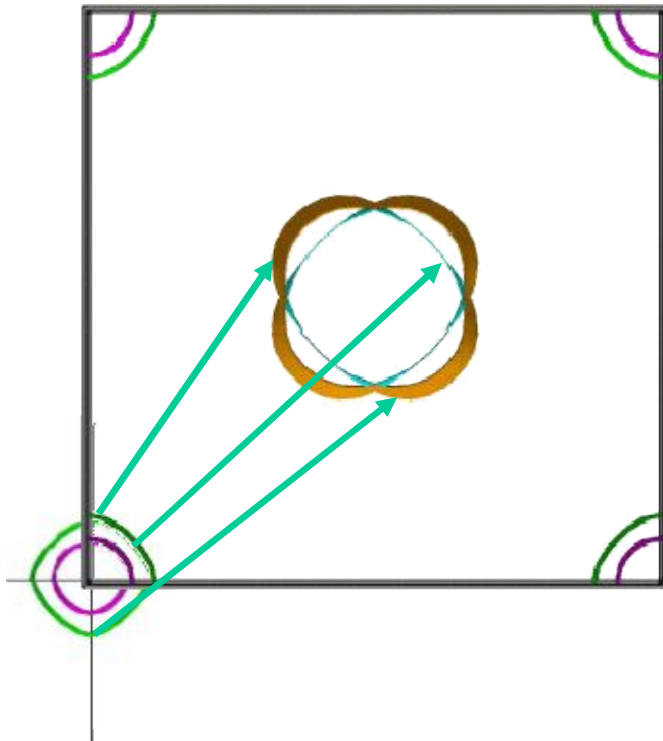
In all actual materials there is some “poor” nesting of the Fermi surfaces .



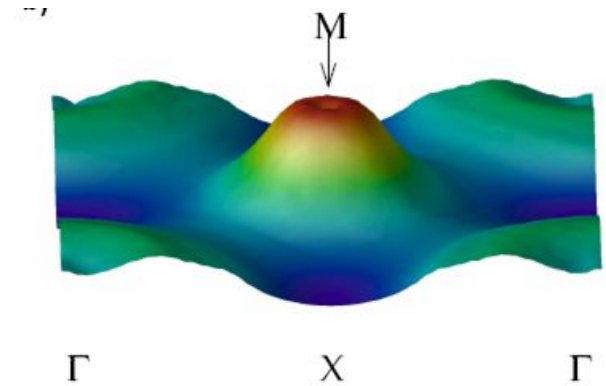
ingredient 2 – spin fluctuation

$$\text{Re } \chi_0(\mathbf{q}, \omega \rightarrow 0) = \sum_{\mathbf{k}} \frac{f_{\mathbf{k}+\mathbf{q}} - f_{\mathbf{k}}}{\varepsilon_{\mathbf{k}+\mathbf{q}} - \varepsilon_{\mathbf{k}}}$$

$$\frac{\text{Im } \chi_0(\mathbf{q}, \omega)}{\omega} \Big|_{\omega \rightarrow 0} = \sum_{\mathbf{k}} \delta(\varepsilon_{\mathbf{k}+\mathbf{q}} - E_F) \delta(\varepsilon_{\mathbf{k}} - E_F)$$



$\text{Im } \chi_0(\mathbf{q}, \omega)/\omega \Big|_{\omega \rightarrow 0}$



$\text{Re } \chi_0(\mathbf{q}, 0)$

fully pairing for the s_{\pm} state (sharp nesting not needed)

FOUND EXPERIMENTALLY!



Experimental status

Pairing symmetry:

- definitely singlet
- nearly definitely not d
- most likely sign-changing
- strong evidence for s_{\pm} (even though only indirect so far)



Pairing glue, after all?



There is infinite number of incorrect theories, correctly describing the finite number of experimental facts.

(ascribed to Niels Bohr)

The concept of pairing glue appears to work reasonably well in both cuprates and pnictides (even predictively!), as opposed to all other methodologies, despite the drastic difference between the two families – a big feather in the pairing glue proponents' hat.



“Iron age” Matthias rules

1. A high symmetry is good; cubic symmetry is the best.

new rule: Layered structures are good

2. A high density of electronic states is good.

new rule: the carrier density should not be too high (compared with, say, conventional metals)

3. Stay away from oxygen.

new rule: 3d metals (V, Cr, Mn, Fe, Co, Ni, Cu) are good.

4. Stay away from magnetism.

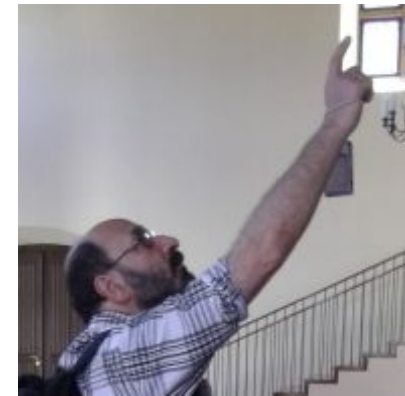
new rule: magnetism is essential

5. Stay away from insulators.

new rule: proper Fermi surface geometry is essential (it must match the structure of the spin excitations)

6. Stay away from theorists.

new rule: enlist theorists, at least to compute the Fermi surfaces (I hope theorists are more useful than this but do not dare to insist).



The theoretical oriented scientist cannot be envied, because nature, i.e. the experiment, is a relentless and not very friendly judge of his work. In the best case scenario it only says "maybe" to a theory, but never "yes" and in most cases "no". If an experiment agrees with theory it means "perhaps" for the latter. If it does not agree it means "no". Almost any theory will experience a "no" at one point in time - most theories very soon after they have been developed.

Title: Theoretical remark on the superconductivity of metals

Authors: [Albert Einstein](#)