

# Black holes, high-energy scattering, and locality

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4th International Sakharov Conference

There has been much discussion of the  
BH information paradox.

Message #1:

Message #2:



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BH information paradox.

Message #1:

Take it seriously!

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Message #1:

Take it seriously!

Message #2:

Can it teach us something about  
quantum-mechanical gravity?



My current viewpoint: this could play an important guiding role, analogous for example to the instability paradox in going beyond the classical model of the atom

arXiv:0705.2197

The paradox:  
Hawking, 1974

What happens to information that falls  
into a black hole?

Emitted in evaporation: *locality forbids*

Destroyed: *violent energy nonconservation*

Preserved (remnant): *infinite production  
instability*



# The paradox: a conflict between

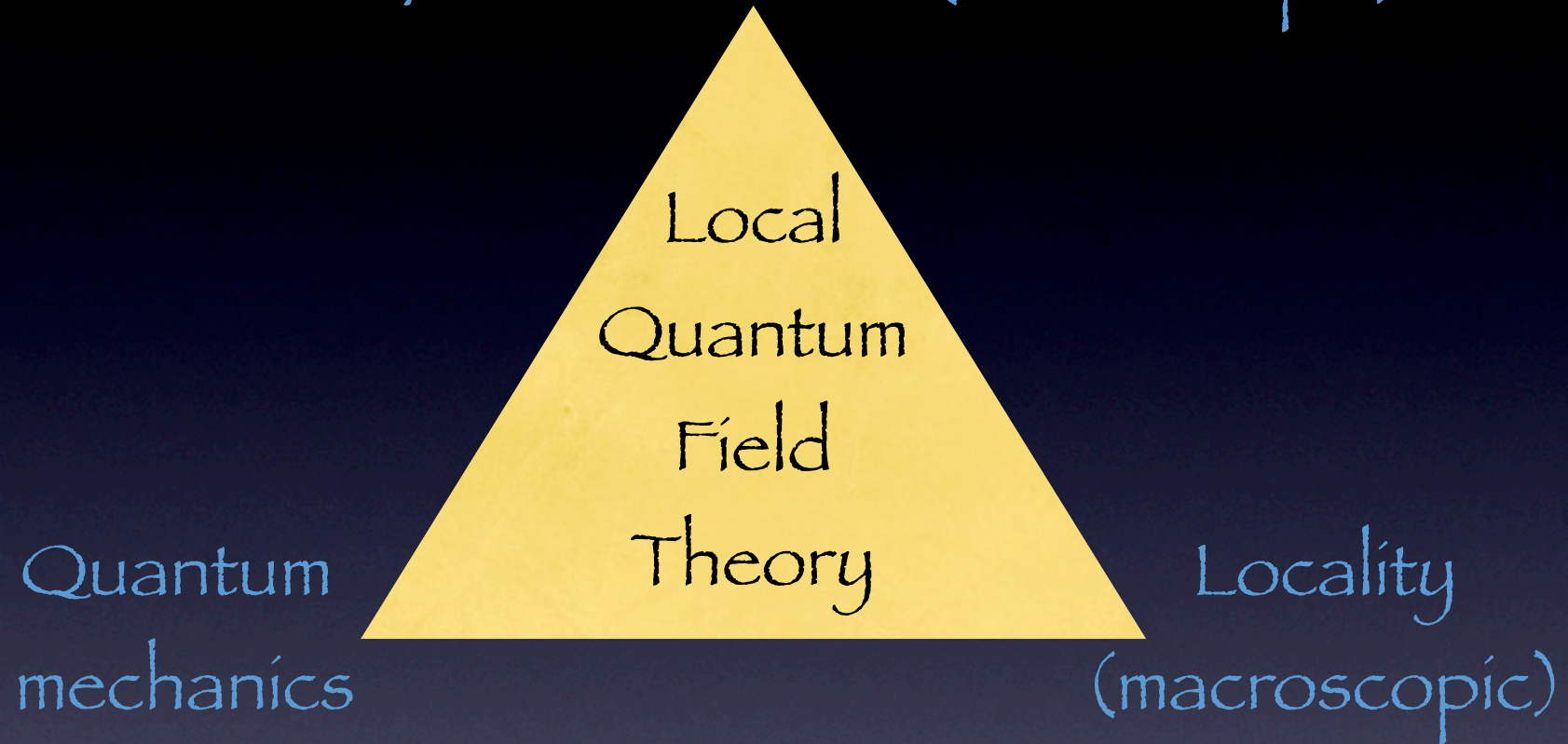
Lorentz/diff invariance (macroscopic)

Quantum  
mechanics

Locality  
(macroscopic)

# The paradox: a conflict between

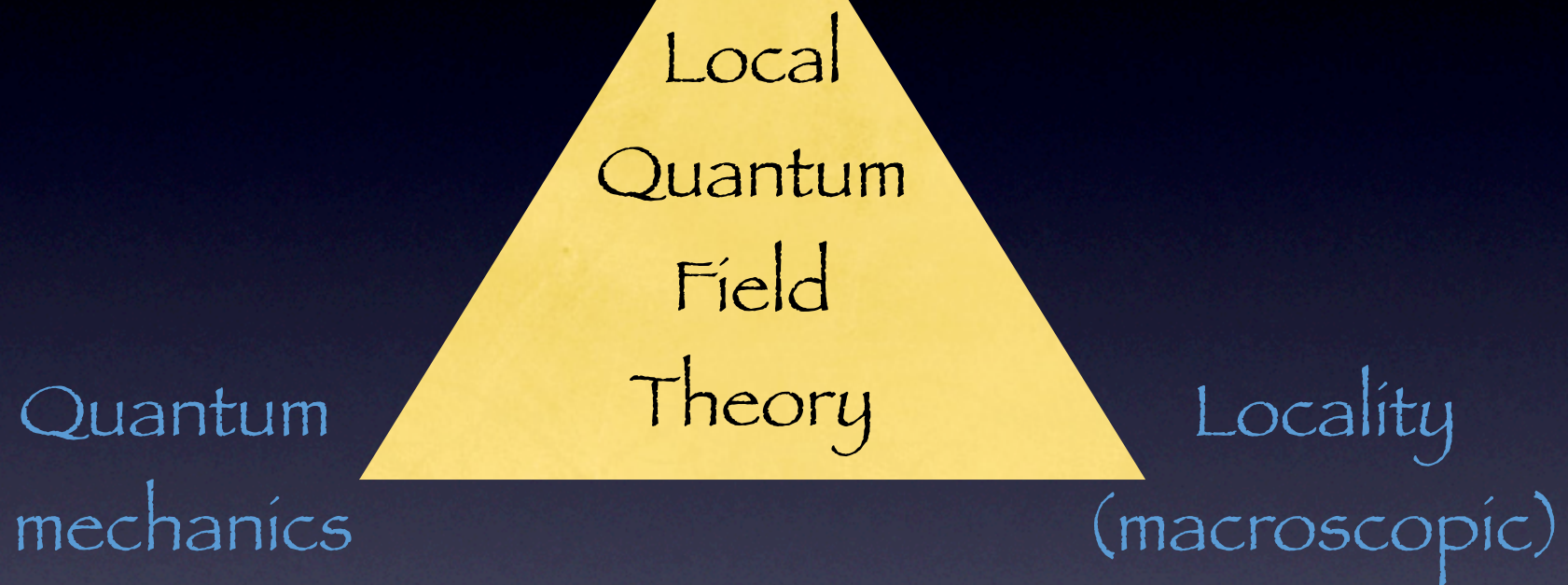
Lorentz/diff invariance (macroscopic)





# The paradox: a conflict between

Lorentz/diff invariance (macroscopic)



Working assumptions:

- 1) QM -- hard to consistently modify
- 2) LI -- hard to modify (symm of  $S$ -matrix)

A growing sense: *modify locality* (at least)



A growing sense: **modify locality** (at least)

proposals:

- historical order ↓
- “Quantum foam”
  - String extendedness
  - Horizon scale nonlocality  
(SBG, hep-th/9203059)
  - Holographic principle;  
AdS/CFT
  - ...

These are different, and not entirely  
complete pictures.

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1) Where does locality break down?  
parametrize correspondence boundary

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- 1) Where does locality break down?  
parametrize correspondence boundary
- 2) What is the mechanism?



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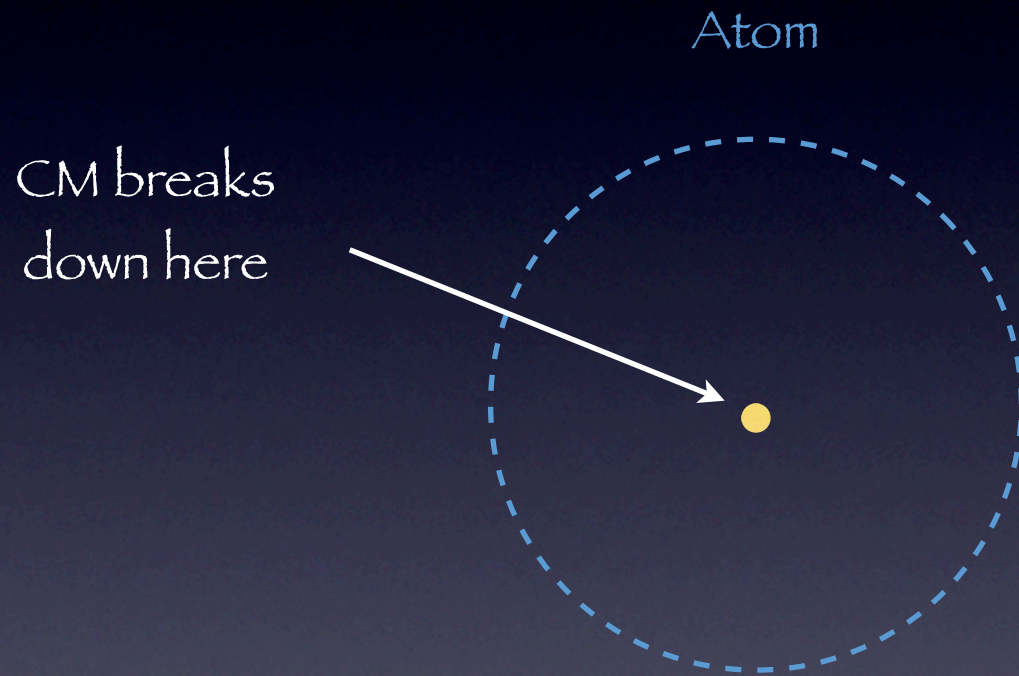
Need a more precise characterization:

- 1) Where does locality break down?  
parametrize correspondence boundary
- 2) What is the mechanism?
- 3) What physical/mathematical framework replaces QFT, and how might locality emerge from it in familiar contexts?

Possible analogy from history:  
“classical instability paradox”

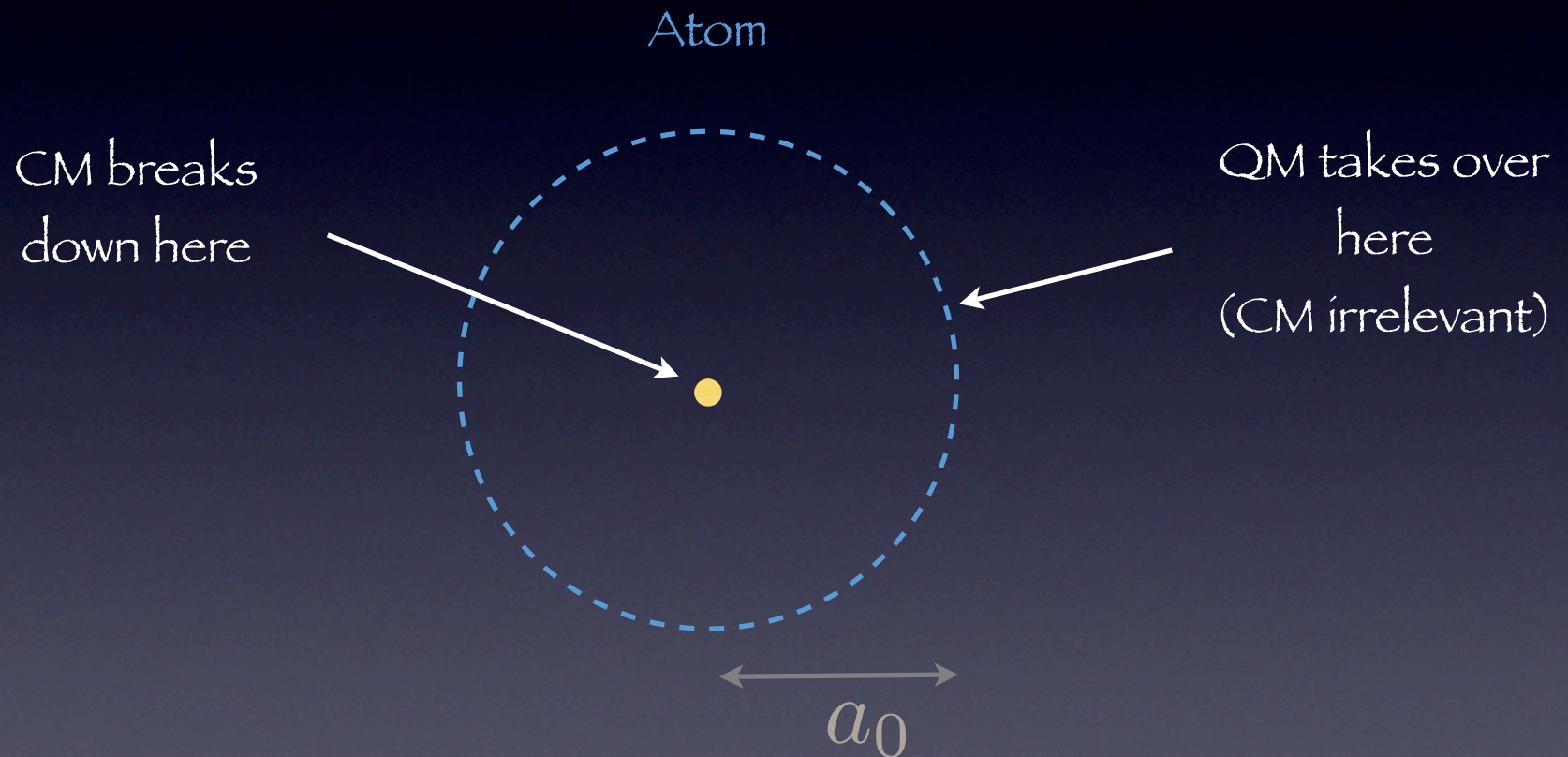


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(big surprise: new principles at  $a_0 \gg r_N$  )



# Breakdown of classical mechanics:

1) Where fails:  $\Delta x \Delta p = 1$  (~~phase space~~)

(correspondence boundary)

2) Mechanism: wave behavior of matter

classical phase space  $\longrightarrow$  quantum wavefunction

3) Framework: Hilbert space; Schrodinger/  
Heisenberg mechanics

# Some possible proposals for a correspondence boundary for gravity:

planckian curvature:

$$\mathcal{R} < M_P^2$$

string uncertainty principle:  
(Veneziano/Gross)

$$\Delta X \geq \frac{1}{\Delta p} + \alpha' \Delta p$$

modified dispersion:

$$p < M_p$$

} 1 particle

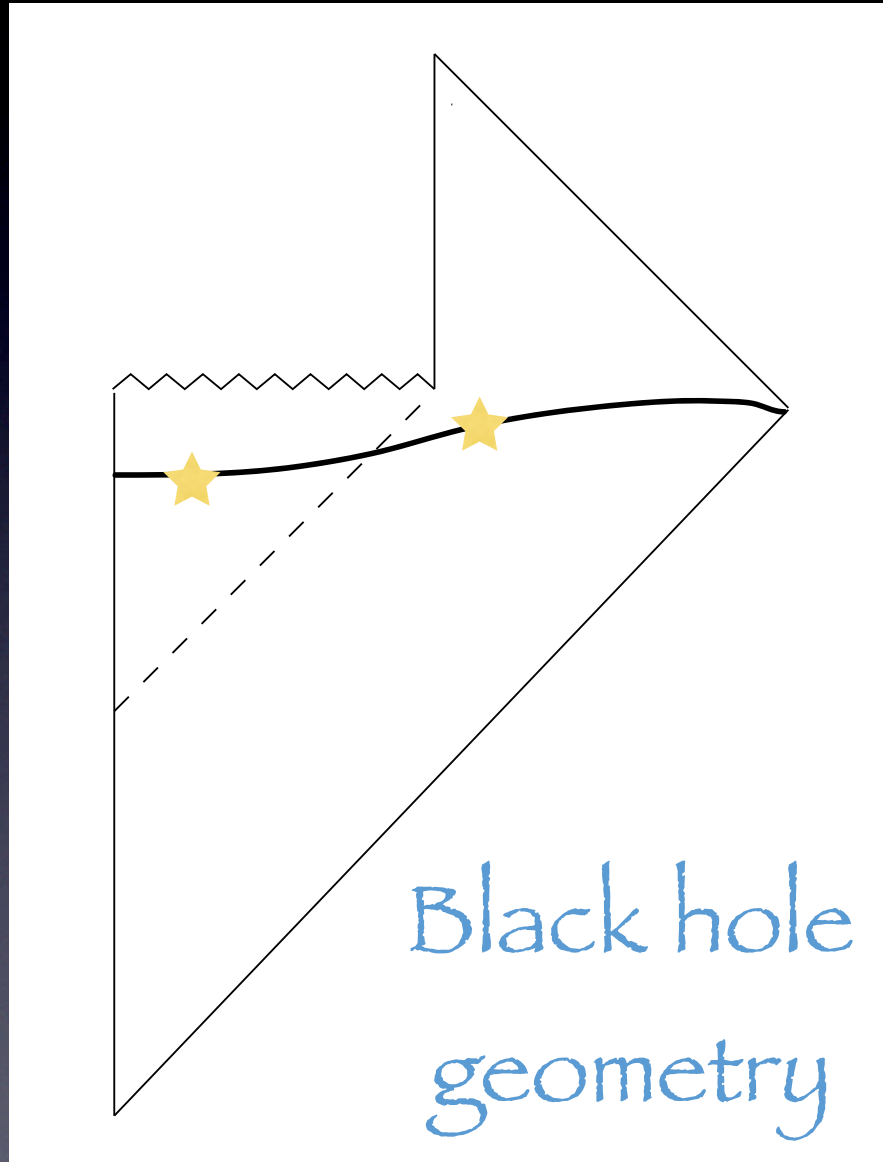
holographic (information)  
bounds:

$$S \leq A/4G_N$$

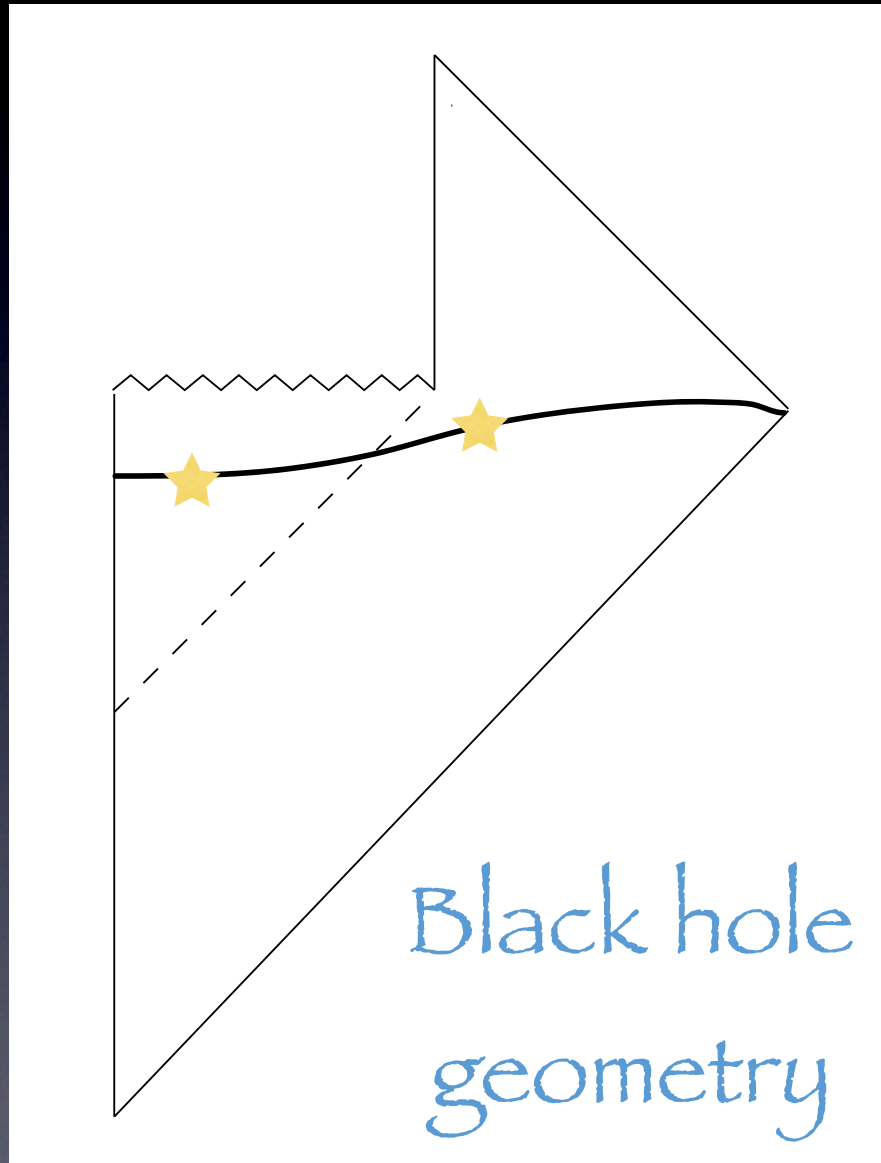
multiparticle



A hint from the “inside” perspective:



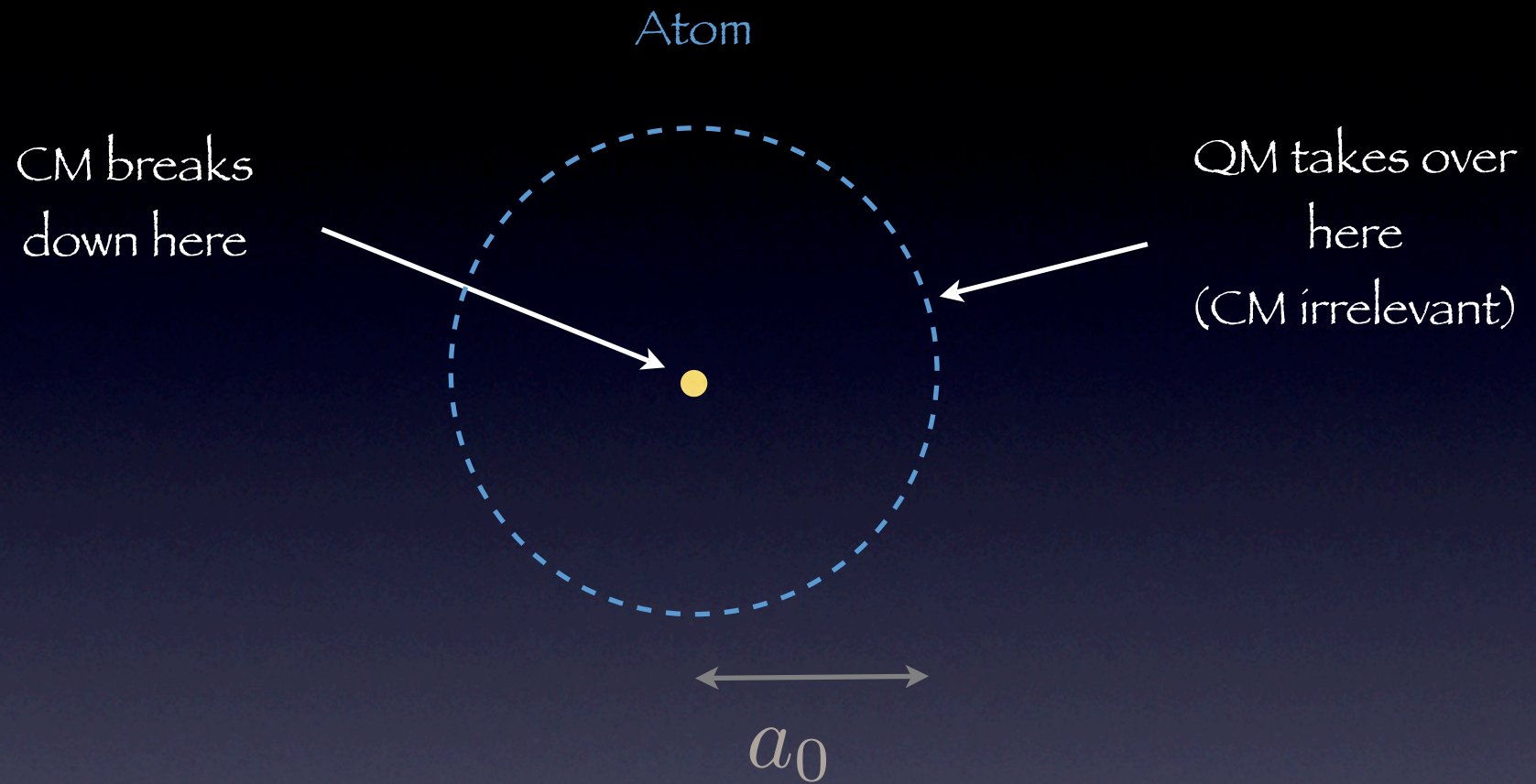
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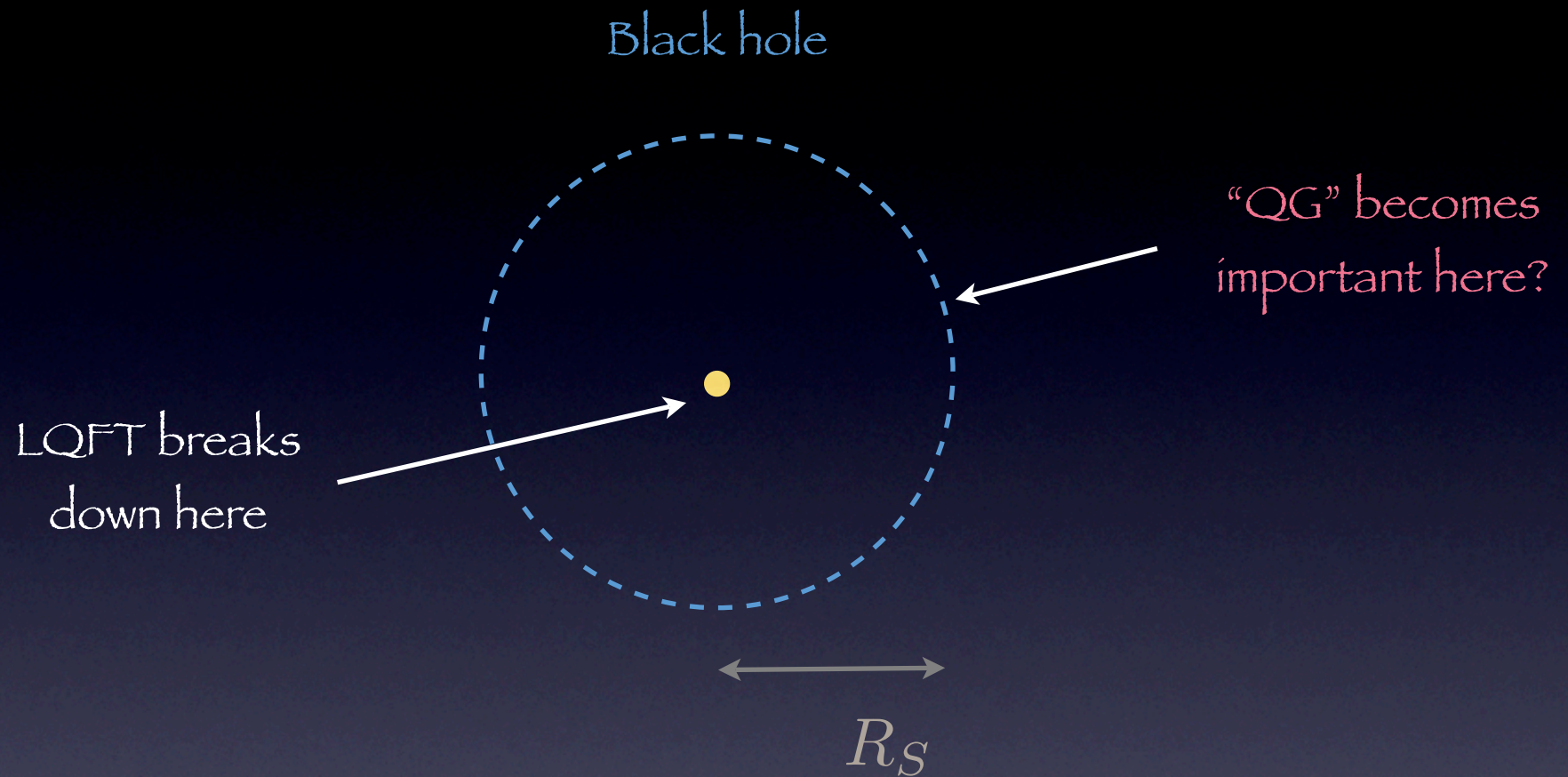
nonlocality needed  
on scale  $\sim R_S$  ?



# The atomic analogy:



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Will suggest: take more literally: new principles at  $R_S$



# Probes of locality:

- local observables
- high-energy scattering

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- high-energy scattering

where does present framework break down?

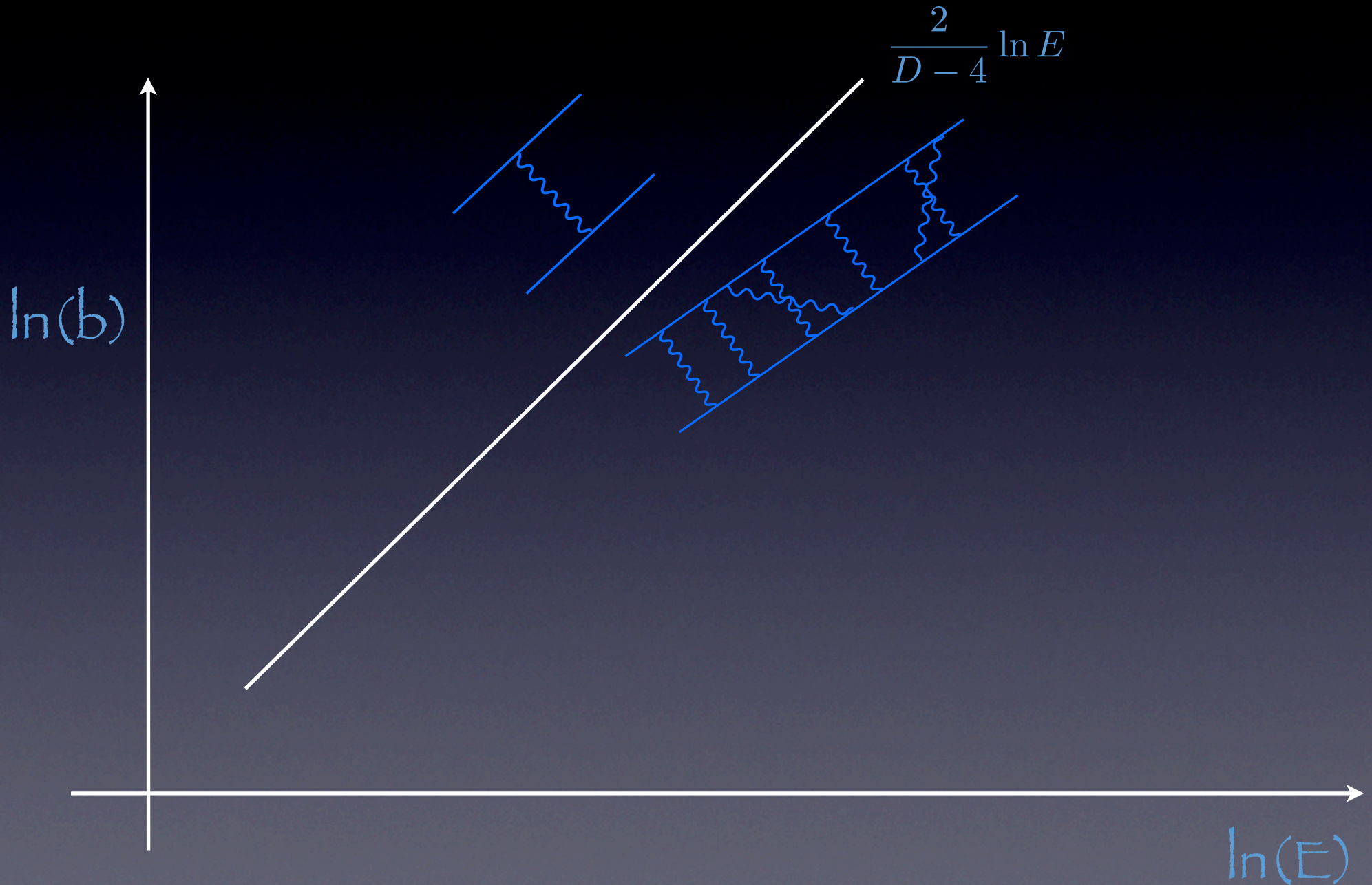
origin of important corrections?

(bear in mind: possible surprises; classical physicist would have never guessed  $a_0$  )



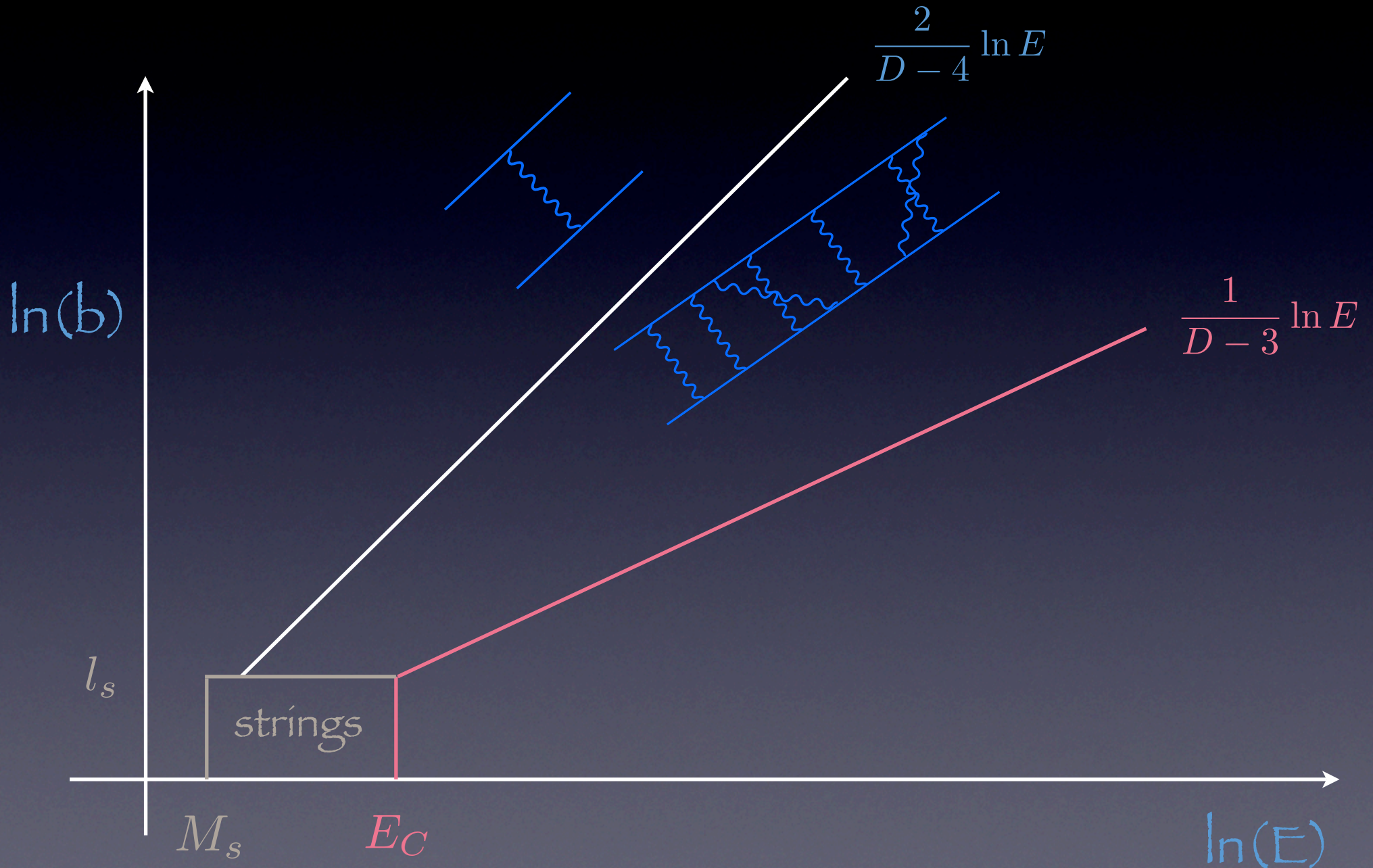
Lessons - Amati, Ciafaloni, Veneziano;  
't Hooft; SBG, Gross, Maharana; ...

consider strings, or  
more generally



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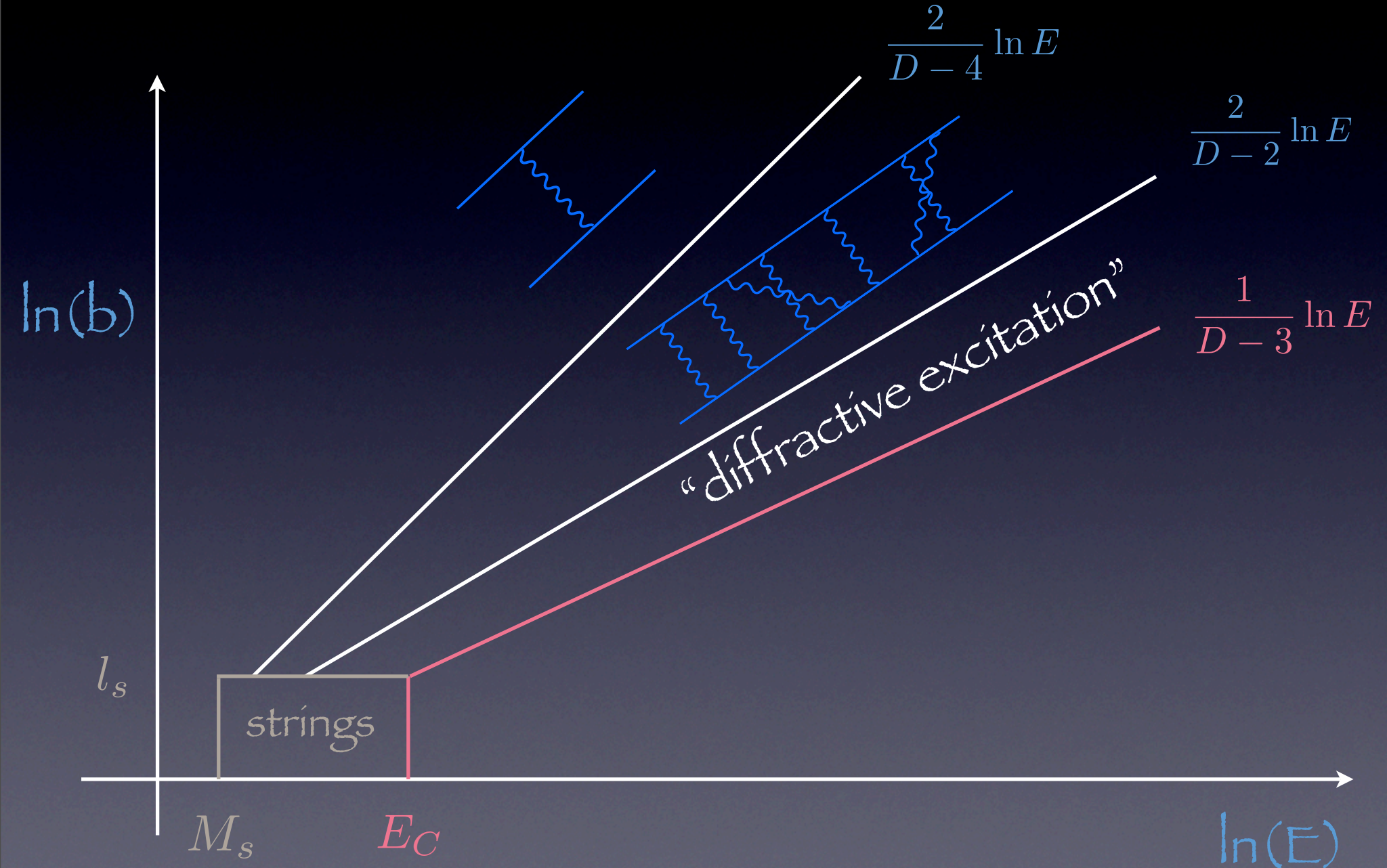
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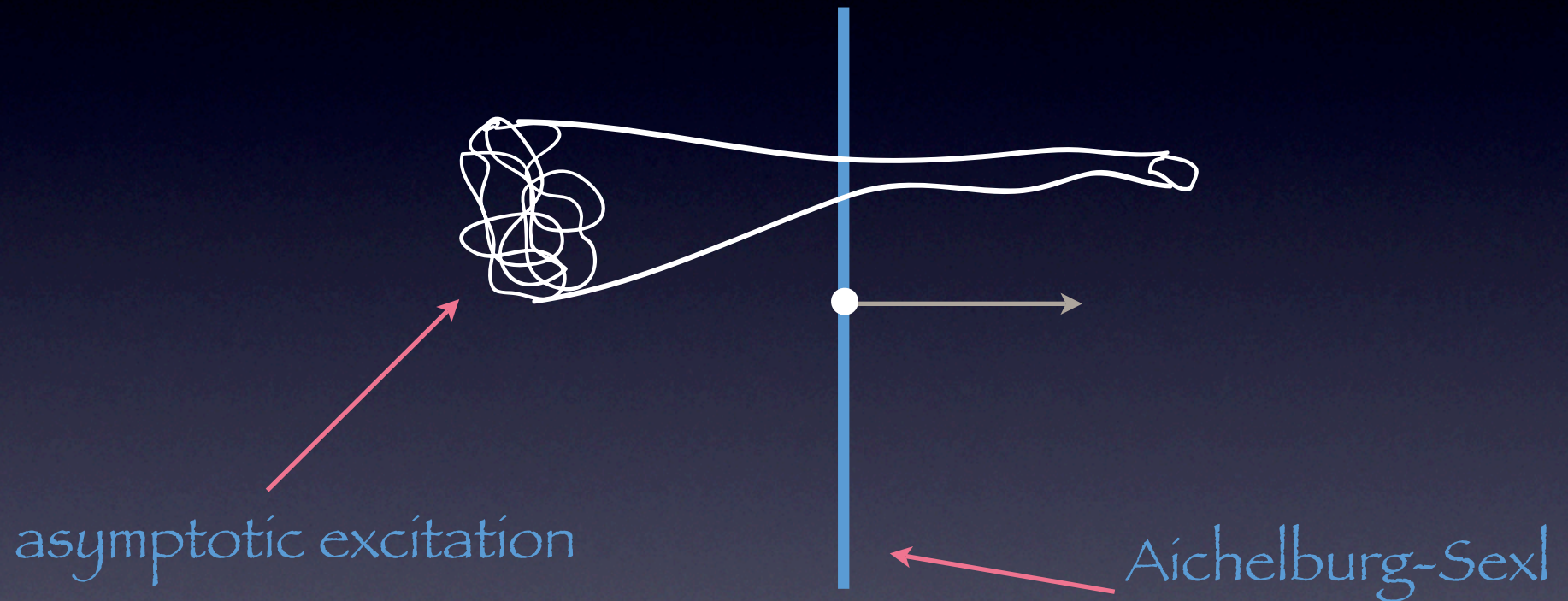


# Q1: understand diffractive excitation

Picture:

hep-th/0604072;

arXiv:0705.1816 w/ Gross and Maharana



“tidal excitation”

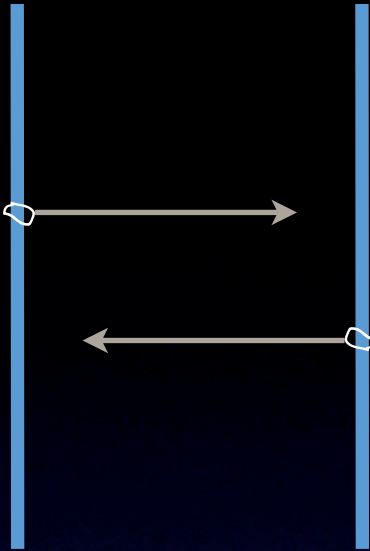


Q2: what happens at  $b \sim R_S(E)$  ?

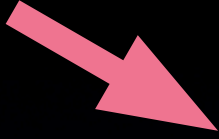
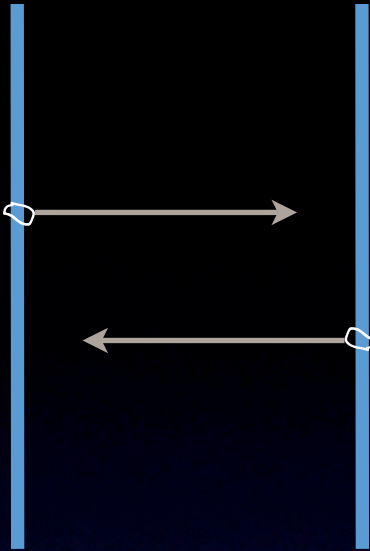
A) stringy effects?

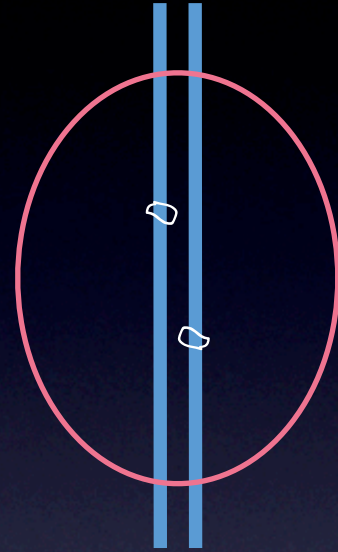
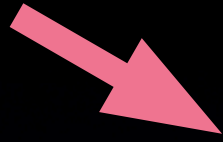
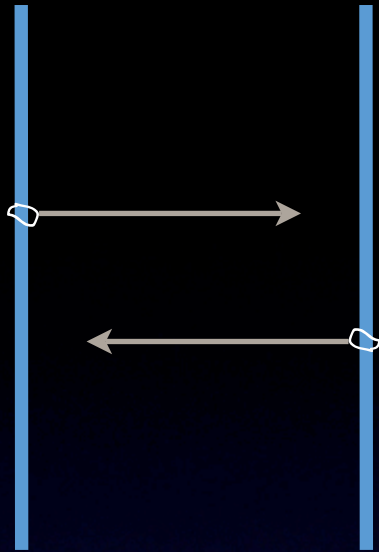
Debates/discussions with  
Gross (and others);

Our discussion converged in writing  
GGM:



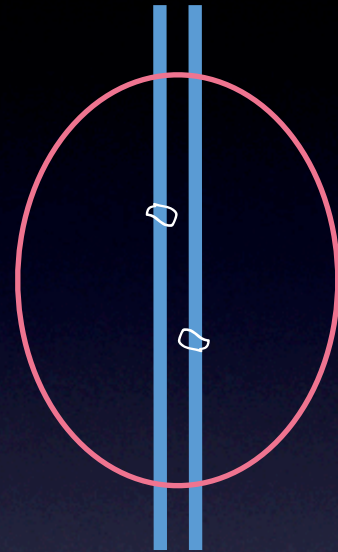
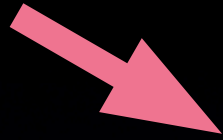
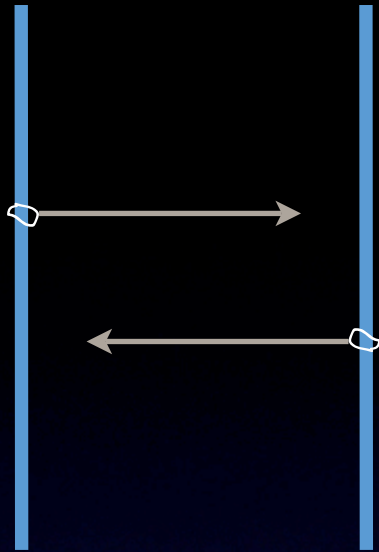






Trapped  
surface





Trapped  
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Black hole

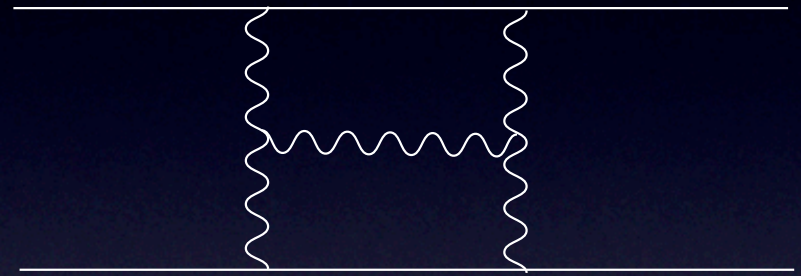
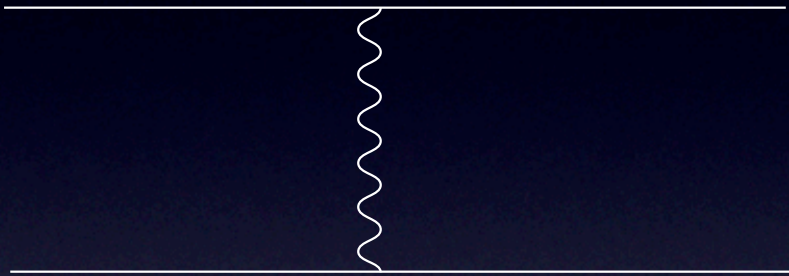


Different timescales  
No role for extendedness?

B) What effects are relevant?



## B) What effects are relevant?



$$1 + \mathcal{O} \left[ \left( \frac{R_S(E)}{b} \right)^{2(D-3)} \right]$$

- Perturbation theory apparently breaks down

- This divergence is not short distance

- Renormalizability (or order-by-order finiteness) doesn't resolve it!

(Indication: unitarity is perhaps a more fundamental issue than renormalizability in gravity?)

This suggests some proposals:



1) Proposed correspondence boundary  
(or piece thereof)

dynamical descript.

validity

CM:

$x(t), p(t)$

$$\Delta x \Delta p > 1$$



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# dynamical descript.

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“locality bound”

(generalizations: N-particle; dS)

SBG & Lippert;  
hep-th/0605196;  
hep-th/0606146

2) Proposed mechanism

nonperturbative gravity: delocalization



## 2) Proposed mechanism

nonperturbative gravity: delocalization

e.g. isn't obviously: extended strings (or  
branes)

(correspondingly, clear distinction between “string  
uncertainty principle” and the locality bound)

**Suggestion:** the nonperturbative physics that unitarizes  
gravity in regimes where gravitational perturbation theory  
fails is nonlocal (“nonlocality principle”)

How else to probe these ideas?



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Parameterize our ignorance:

The S-matrix

General properties of scattering,  
consistent with unitary quantum  
evolution, basic properties of gravity

e.g: locality  $\longleftrightarrow$  polynomiality?

SBG and Srednicki;

SBG and Porto, WIP

$2 \rightarrow 2$  scattering:

- for large enough  $D$ , eliminate IR divs in pert. theory.

- so, conjecture amplitudes are well defined in full theory:  $T(s, t)$



# PW expansion:

$$T(s, t) = (\text{const}) E^{4-D} \sum_{l=0}^{\infty} (l + \nu) C_l^\nu(\cos \theta) \left[ e^{2i\delta_l(s) - 2\beta_l(s)} - 1 \right]$$
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Some features:

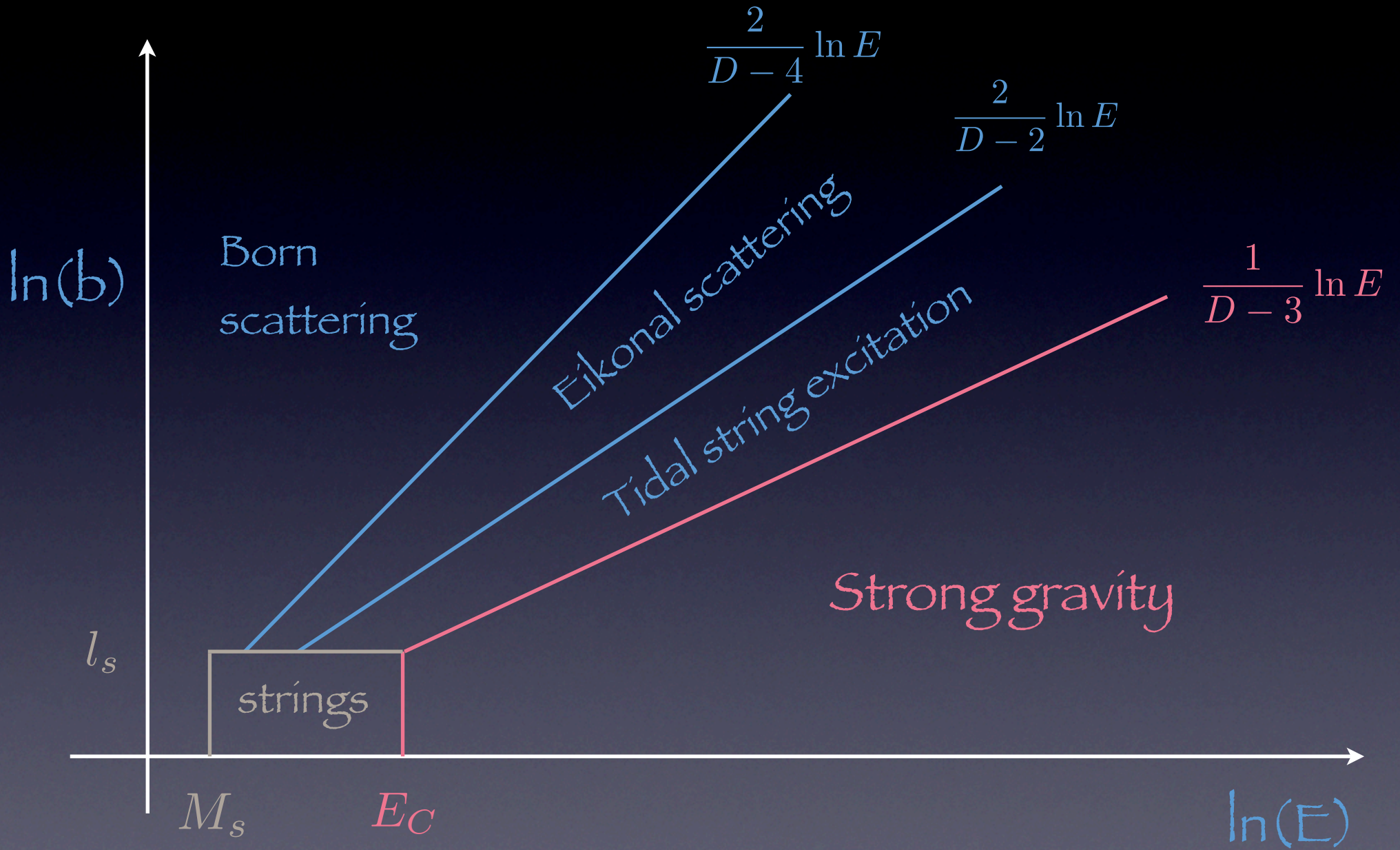
A. Understand Born, eikonal regions

e.g.  $\delta_l \approx [ER_S(E)]^{D-3} / l^{D-4}$

$\beta_l = \text{“unimportant”}$

(though model dependent)





B. Ansatz for BH region

$$l \lesssim ER_S(E) = L$$

$$\beta_l \approx \frac{S(E, l)}{4}$$

(Bekenstein-Hawking entropy -- expected if approx. thermal description)

(likewise, Ansatz (modified) for real part

$$\delta_l(E) \sim \pi S(E, l)$$

- though not critical for following observations?)



## Features:

- both absorptive and eikonal amplitudes violate Froissart; e.g.

$$\sigma_{BH} \sim [R_S(E)]^{D-2}$$

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- related point, amplitudes not polynomial:

$$T(s, t) \sim e^{s^\alpha t^\beta}$$

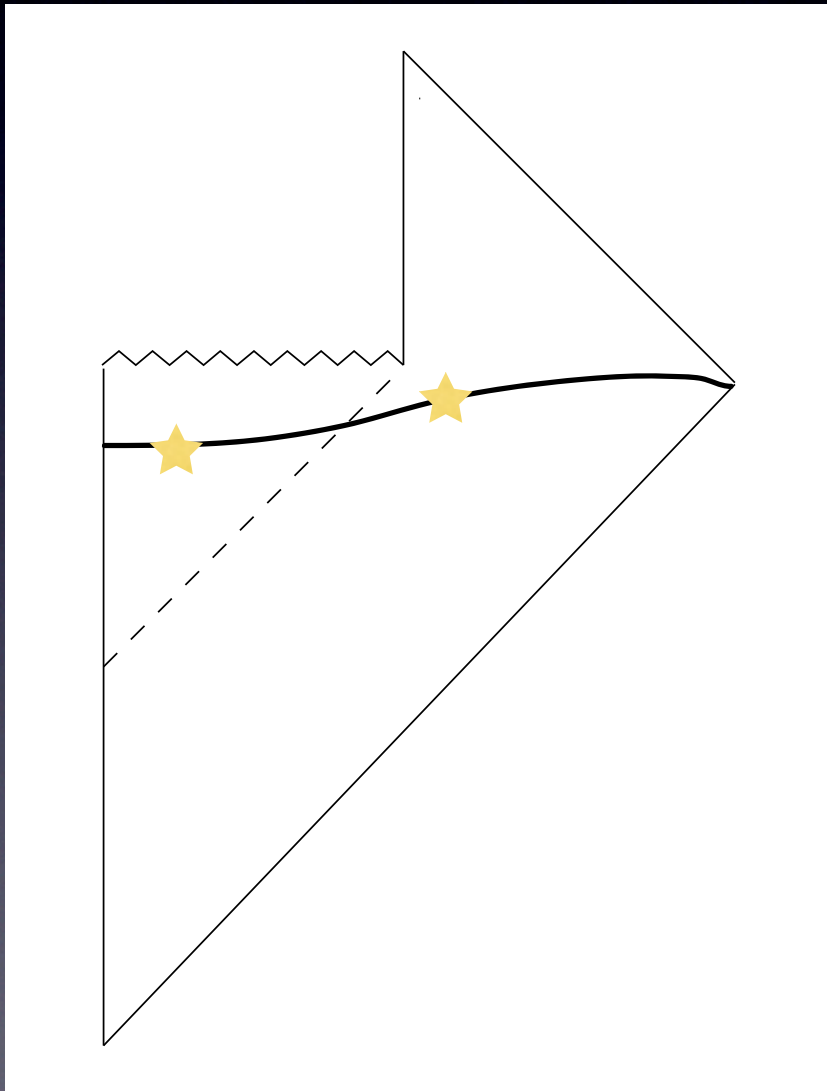
plausibly associated w/ lack of usual locality?

- (amplitudes apparently obey Cerulus-Martin -- contrary to earlier expectations)



Another way to probe these ideas:

Where did Hawking go wrong?



“Nice slice argument”

inside viewpoint

apparently require  
nonlocality on scale  $\sim R_S$

A) perhaps the correct theory simply doesn't accurately describe the collection of nice slice states, just as quantum mechanics doesn't accurately describe phase space at  $\Delta x \Delta p < 1$

(though, expect approx. description of infalling obs.)



B) See breakdown of QFT+GR on nice slices

some evidence:

([hep-th/0703116](https://arxiv.org/abs/hep-th/0703116))

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i) Nice slice states **not observable** without a large perturbation of the semiclassical geometry

(a less positivistic statement than used to justify complementarity!)



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ii) Quantization on nice slices: fluctuations and large backreaction

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ii) Quantization on nice slices: fluctuations and large backreaction

both by:  $t \sim R_S S_{BH}$



More precise investigation:

Need to understand ( $\sim$ ) local  
observers/observables

(diff. invariance: no exact local observables)

... also for cosmology!

# Relational approach (Thursday talk):

“proto-local observables”

see: SBG, Marolf, Hartle;

Gary & SBG: 2d, concrete

Basic idea:

$$\mathcal{O} = \int d^4x \sqrt{-g} B(x) O(x)$$
$$\langle B(x) \rangle = b(x)$$

for appropriate background:  $\langle \mathcal{O} \rangle \approx O(x_0)$

localization relative to background

- exploring in cosmological contexts

e.g. dS: SBG & Marolf and WIP



- localization only *approximate*

- e.g.: fail to reproduce local obs. when locality bd. violated

- thus, fits with the notion that usual notion of locality is not exact in gravity

Other ways to proceed?



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AdS/CFT or Matrix: dual theories

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AdS/CFT or Matrix: dual theories

Warmup: can extract the flat-space  $S$ -matrix?

arXiv:0903.4437 w/ Gary & Penedones: Some success  
(plane wave lim.)

arXiv:0904.3544 w/ Gary: Some apparent limitations  
(another talk...)

How can string theory address these questions?



More generally:

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How can we have a theory:



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1) Consistent ( $\sim$ causal)

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4) Nearly-local

(i.e. behaves locally in usual low-energy circumstances)



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A highly non-trivial set of conditions to satisfy!

Might this help guide us to such a “Non-Local (but Nearly-Local) Mechanics”?

## Approaches:

1) Better understanding of properties of S-matrix

(WIP w/ Porto)

2) Investigate other general aspects of theory

e.g. one small piece: generalize QM sufficiently  
to not require spacetime input

a very modest suggestion in this direction:

arXiv:0711.0757: ~ generalization of S-matrix

framework; apply to cosmology, etc.

relational/proto-local observables

...



# What should we conclude?

1) Multiple considerations (HE scattering; observables; BH information, ...) suggest modification of conventional notion of locality - *at long distances.*

possible slogan:

“unitarity restored at the price of locality”

(though the nonlocality may be less radical than some aspects of holography?)

## 2) Mechanism:

- no obvious role for string extendedness
- non-perturbative gravity: not local by usual measures



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- no obvious role for string extendedness
- **non-perturbative** gravity: not local by usual measures
- not clear how any existing model for QG addresses these issues?

Likely not “quantum gravity” -- i.e. quantized version of geometry. **too local, too classical, ...**

Not yet clearly addressed in string theory  
(important to understand if could be)

3) In what circumstances does locality fail?

modest proposals for part of “correspondence boundary” for such a “nonlocal (but “nearly-local) mechanics:”

locality bound, and other related bounds



## 4) General principles?

*Very* modest steps: properties of HE scattering;  
proto-local observables; appropriate generalization  
of QM

*It is important to:*

- ask the right questions
- discard superfluous constructs

*Apparently non-trivial constraints:  
locality without locality, ...*