



# The role of chaos in secular evolution of galaxies

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# Plan of talk

- Non-integrability of motion in galactic models
- Methods of global analysis of phase space structure
- Resonant orbits and their importance for global dynamics
- Astrophysical applications
  - stability of triaxial cuspy galaxies
  - centrophilic orbits and feeding of supermassive black holes
- A novel method for simulating slow collisionless evolution

# Chaos in galactic dynamics

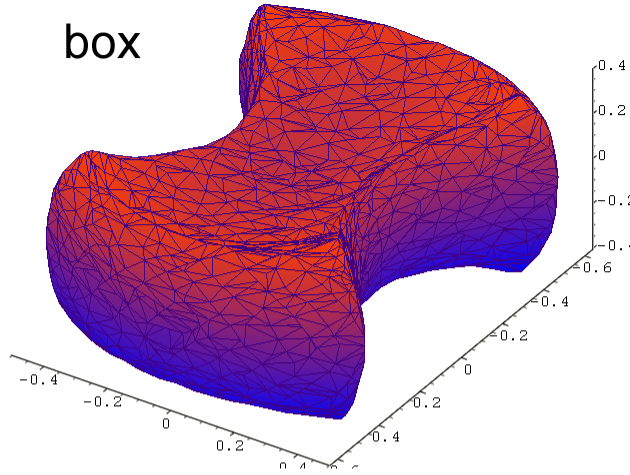
It is often assumed that any reasonable potential is (nearly) integrable. However, there are several important cases when it is not true:

- Triaxial elliptical galaxies with cuspy density profiles
- Spiral non-axisymmetric galaxies around resonances
- Time-dependent potentials

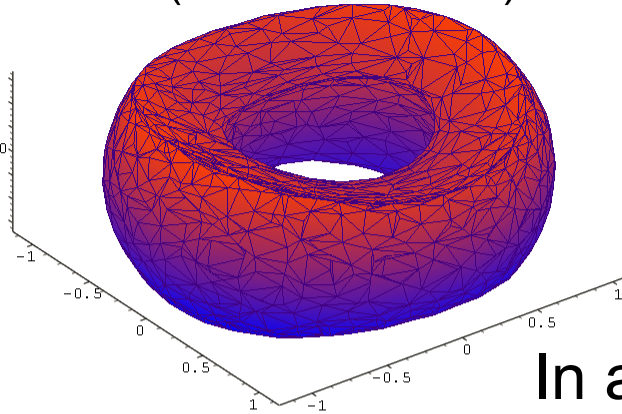
Chaotic orbits exist in 2d potentials, but in 3d they are much more diverse

# Types of orbits in 3d integrable potential

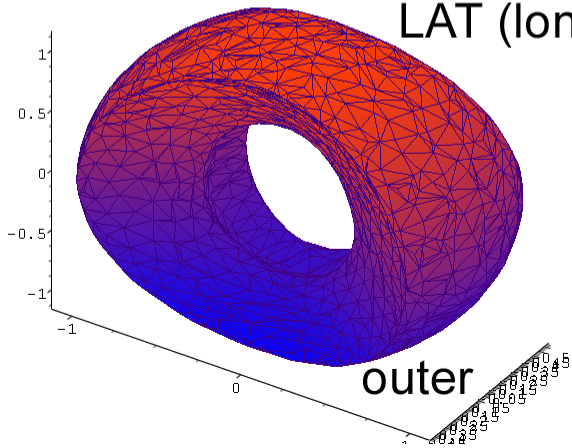
box



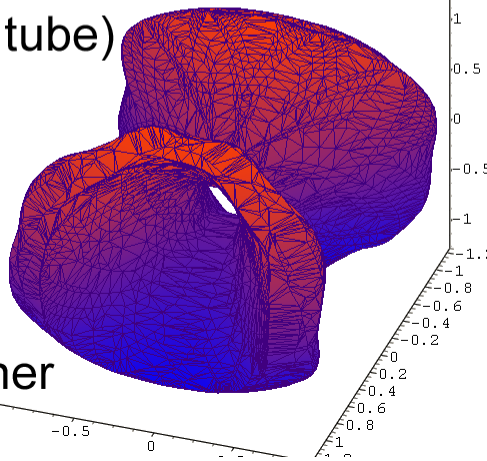
SAT (short axis tube)



LAT (long axis tube)



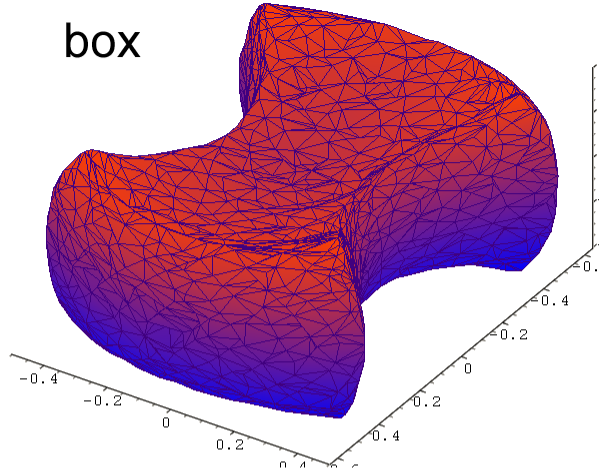
inner



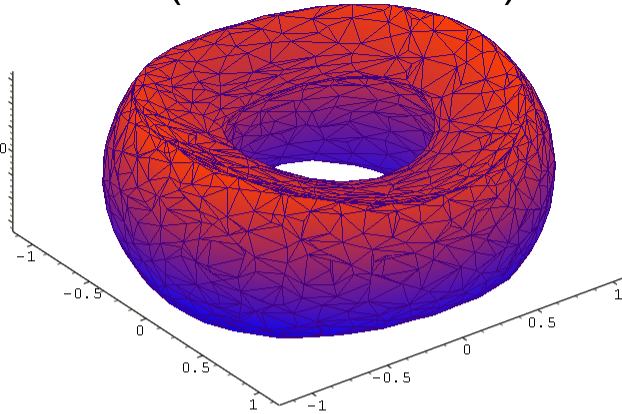
In an integrable potential these are the only possible orbit types

# Types of orbits in 3d non-integrable potential

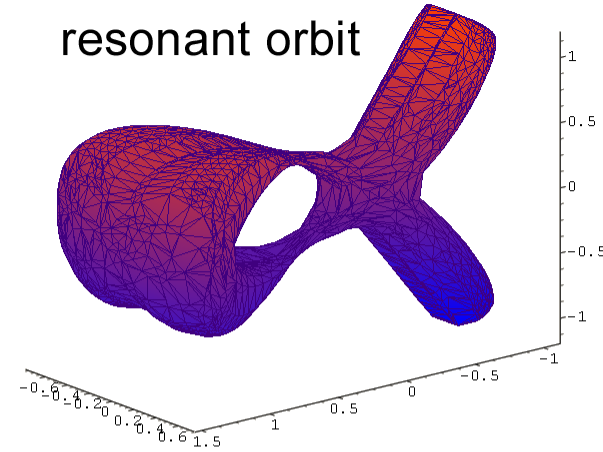
box



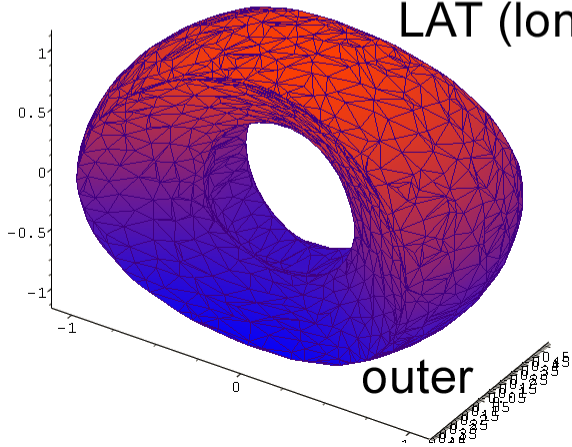
SAT (short axis tube)



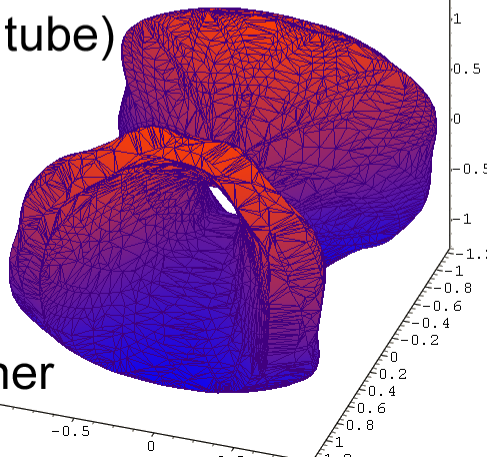
resonant orbit



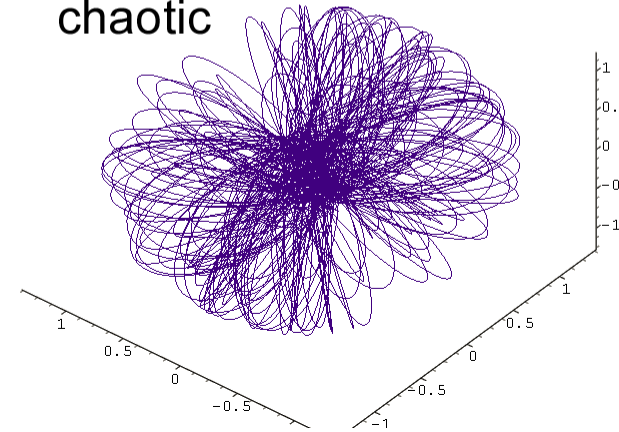
LAT (long axis tube)



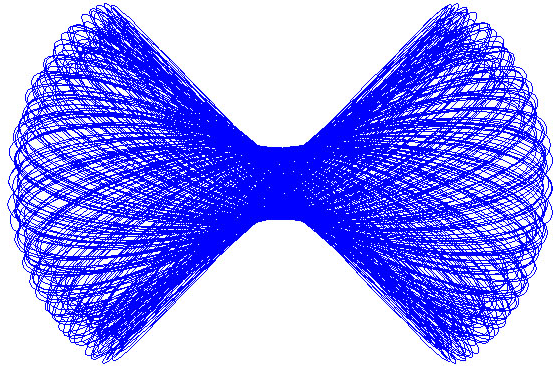
inner



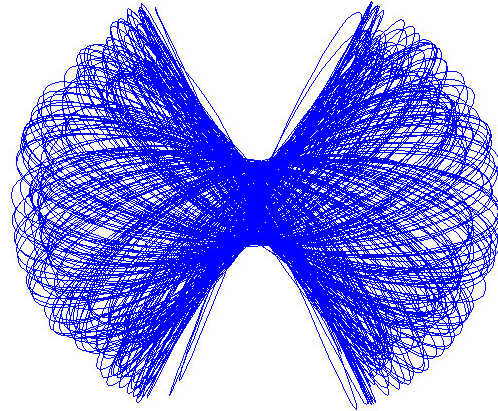
chaotic



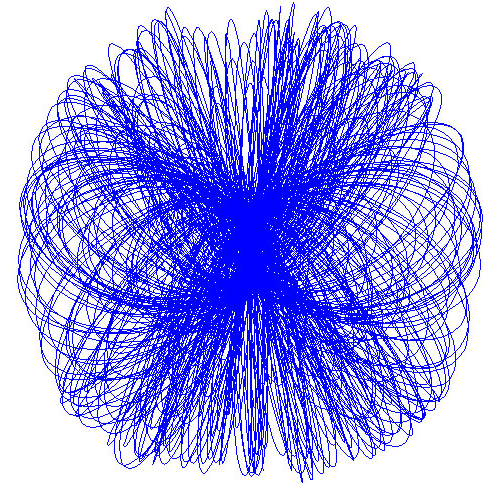
# No well-defined transition to chaos



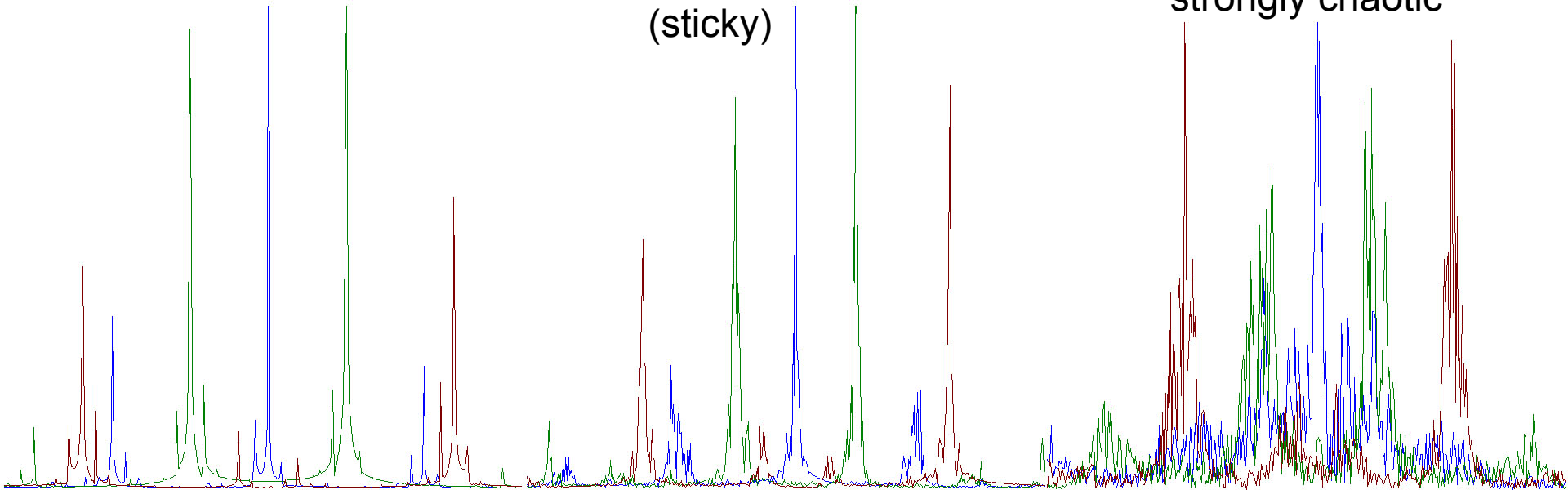
regular orbit



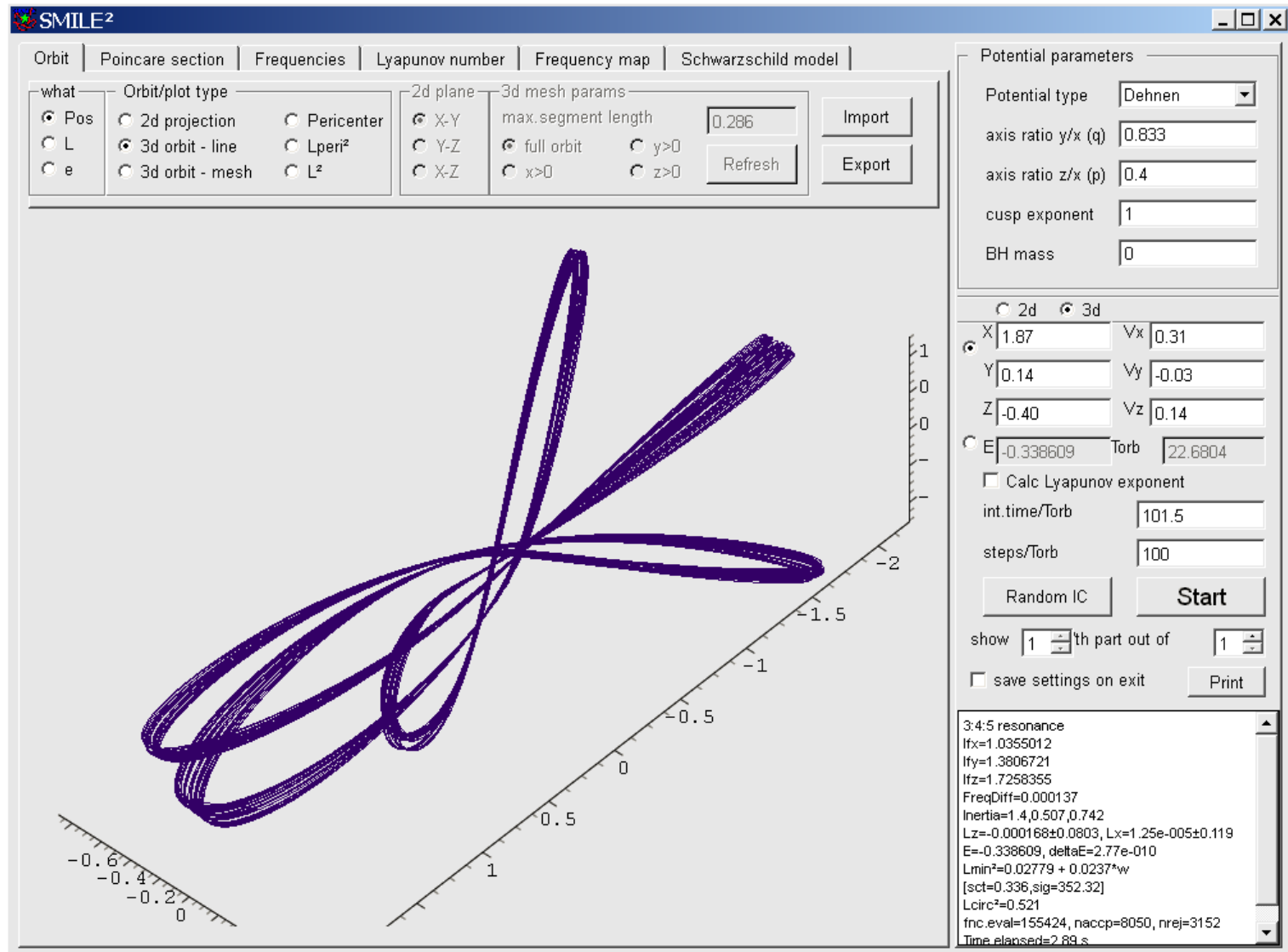
weakly chaotic  
(sticky)



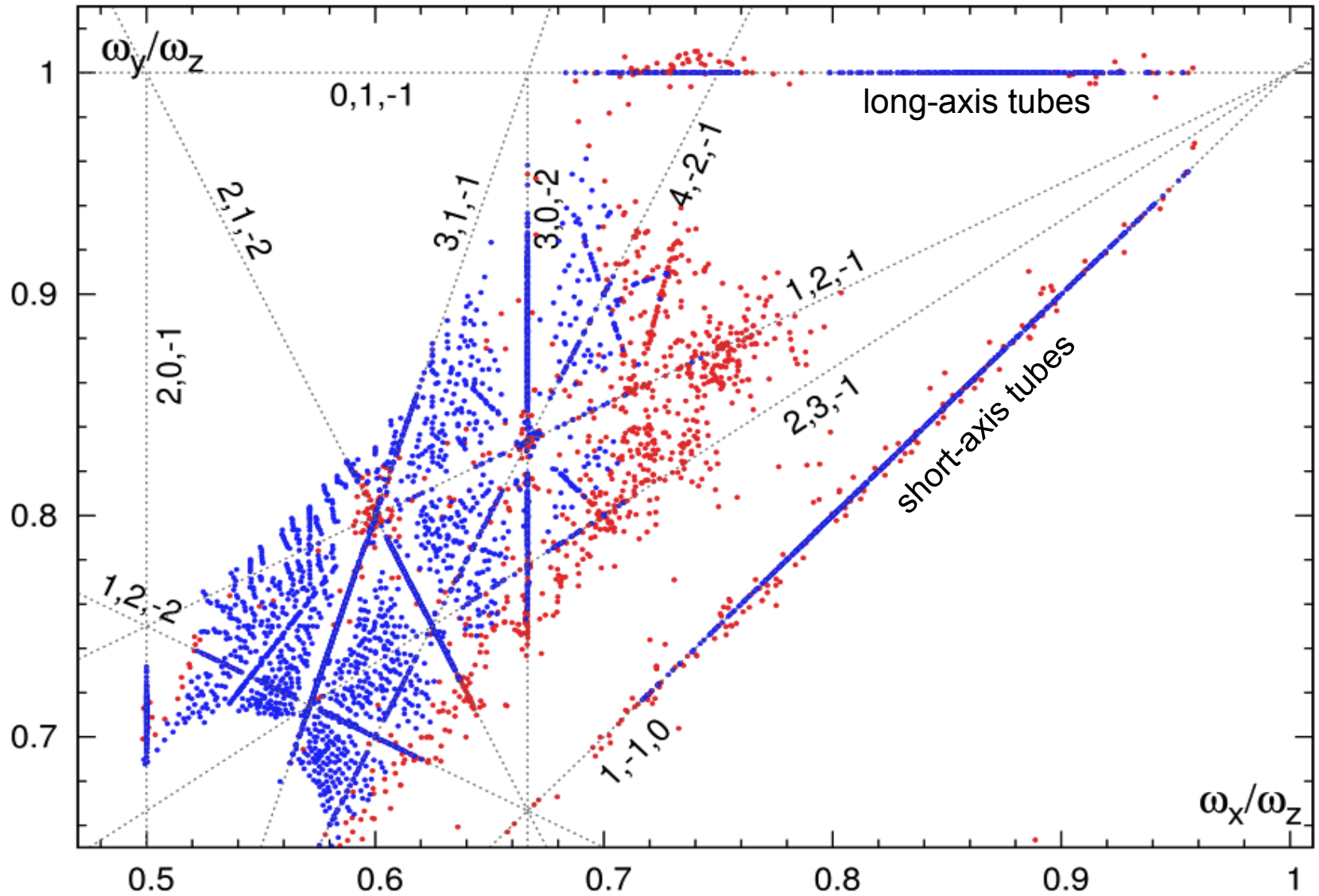
strongly chaotic



# Resonant orbits



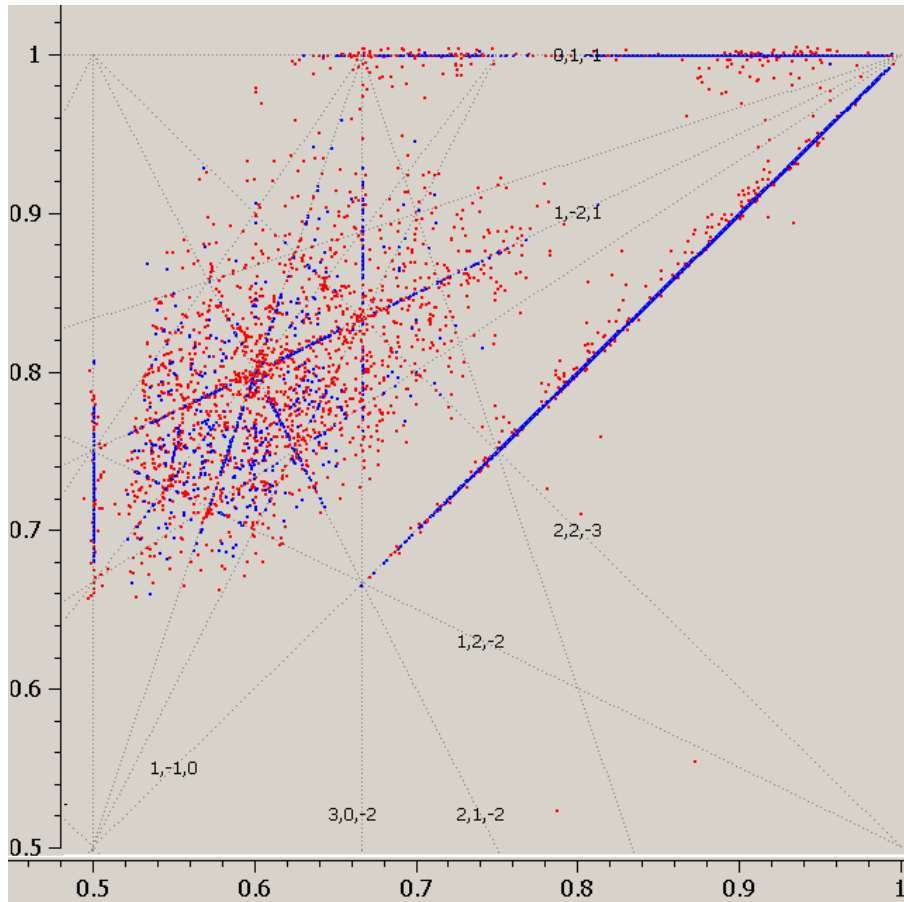
# Frequency maps



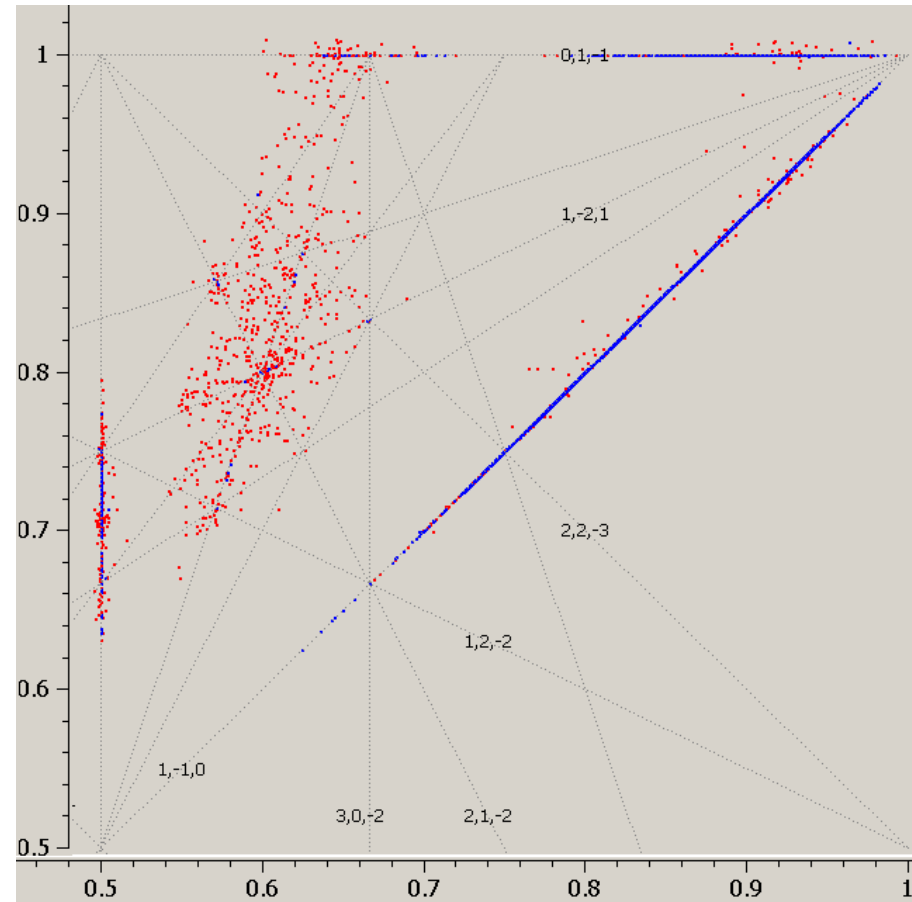


# Frequency maps as tools for studying global dynamics

$\gamma=1$  Dehnen model  
many resonant orbits that create  
the structure of the phase space



$\gamma=2$  Dehnen model:  
almost all non-tube orbits are chaotic;  
no global barriers to chaotic diffusion



# Chaotic diffusion and secular evolution of triaxial cuspy galaxies with supermassive black holes

- Supermassive black holes are efficient "randomizers" of orbits that come close enough to the center of a galaxy
- Chaotic diffusion may lead to secular change of galactic shape
- The number of chaotic centrophilic orbits depends on the degree of triaxiality
- Rates of capture or disruption of stars by the black hole may be substantially enhanced in non-spherical galaxies (compared to spherical case) due to the presence of chaotic orbits
- Secular evolution rate does depend on the cusp slope and BH mass

[Merritt&Quinlan 1998, Valluri&Merritt 1998, Merritt&Poon 2004, Holley-Bockelmann&Sigurdsson 2006, Vasiliev&Athanasoula 2012]

# Interplay between collisional and collisionless effects

- Discreteness noise accelerate diffusion of chaotic orbits through phase space [Kandrup+ 2000s]
- Two-body relaxation in non-spherical potentials enhances the rate of loss-cone repopulation for a supermassive black hole [binary] [Vasiliev&Merritt 2013, Vasiliev,Antonini&Merritt 2013]
- Bottom line: difficult to control collisional effects in simulations of primarily collisionless processes

# A novel method of studying slow collisionless evolution of near-equilibrium models

- Consider evolution of ensemble of  $\mathbf{N}$  orbits (not just *particles*) in the slowly changing potential generated by the time-averaged density of these orbits
- Each orbit is represented by  $\mathbf{m}$  points sampling its trajectory
- Potential and density are evaluated as basis-set expansions with coefficients computed from  $N*m$  points
- Orbits are computed on the time interval  $T \gg T_{\text{orb}}$
- New coefficients of expansion are evaluated from trajectories during the entire integration interval  $T$

# A novel method of studying collisionless evolution

## CONS

- Only suitable for slow evolution of near-equilibrium systems

## PROS

- Beat down discreteness noise in potential  
( $N \cdot m$  instead of  $N$  points are used to compute coefs)
- Time smoothing of potential variation ( $T \gg T_{\text{orb}} \Rightarrow$  adiabatic evolution)
- Computational cost linear in  $N$
- May impose particular form of symmetry (reflection, triaxial, axisymmetric)
- May add random perturbations to velocities during orbit integration that would mimic two-body relaxation rate for a desired  $N_{\text{star}} \neq N$   
(Monte-Carlo collisional evolution code in Spitzer's formulation for **arbitrary geometry**)

# Conclusions

- Chaotic effects are important for many problems of galactic dynamics
- Resonant orbits are important for the global structure of phase space and for the rate of chaotic diffusion
- Frequency map is a useful tool for visualizing this structure
- Possibility of simulating the slow, collisionless evolution in time-smoothed mean-field dynamics